

模拟集成电路设计原理

(Principle of Analog Integrated Circuit Design, INF0130025.02)

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<http://rfic.fudan.edu.cn/Courses.htm>

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反馈

跨阻放大器和电流放大器

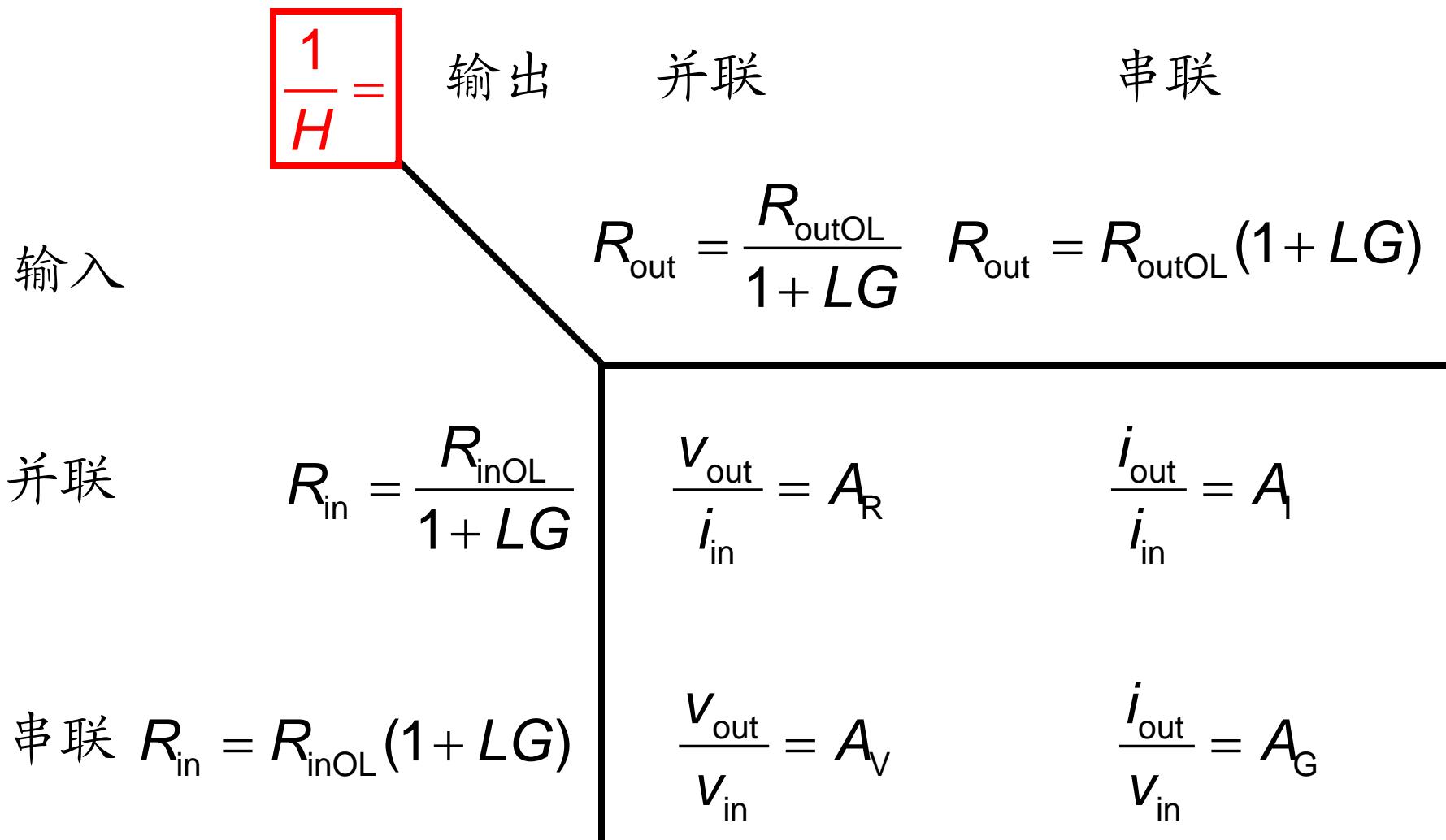
目录

- 导言

- 跨阻放大器的并联-并联反馈
- 电流放大器的并联-串联反馈
- 低噪声和高频的跨阻放大器

Ref.: W. Sansen : Analog Design Essentials, Springer 2006

输入和输出阻抗



目录

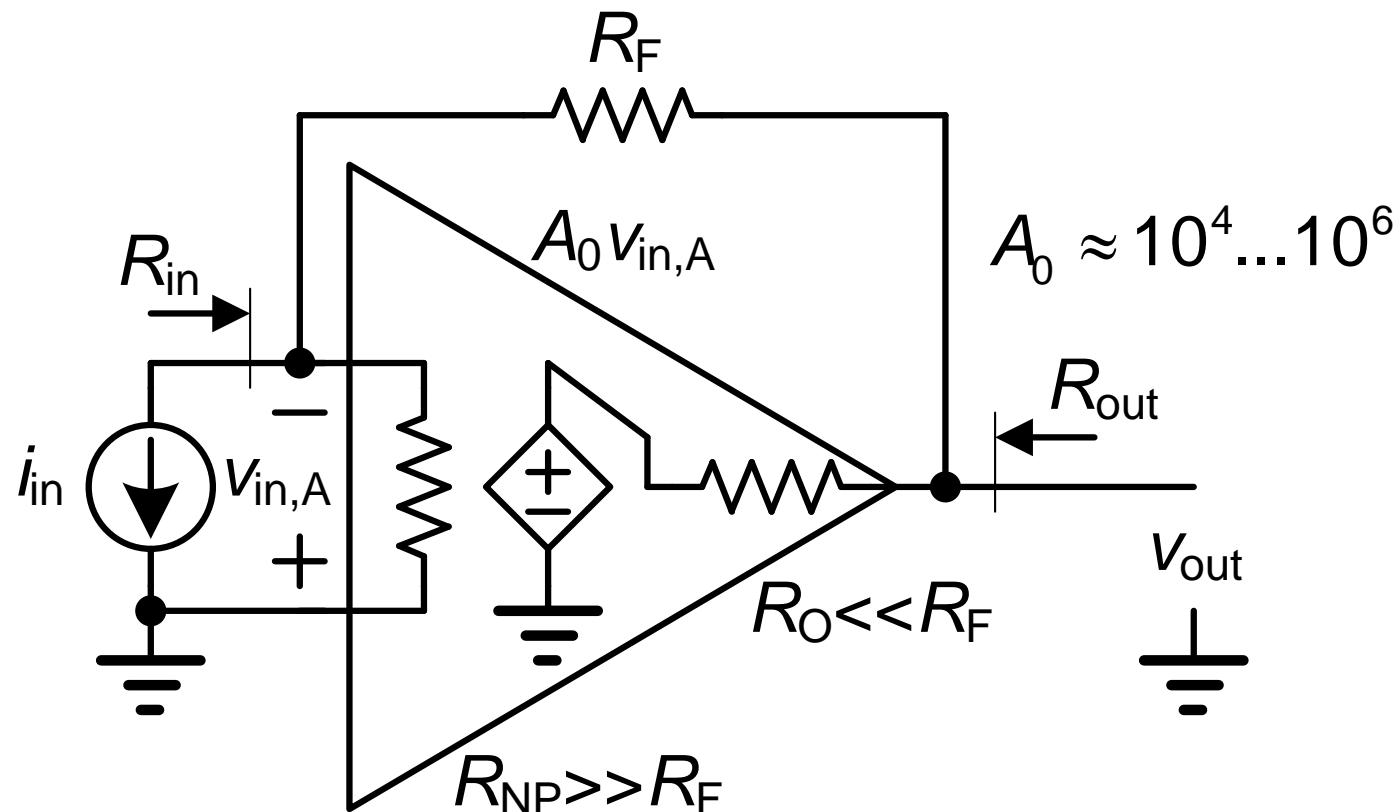
- 导言

- 跨阻放大器的并联-并联反馈

- 电流放大器的并联-串联反馈

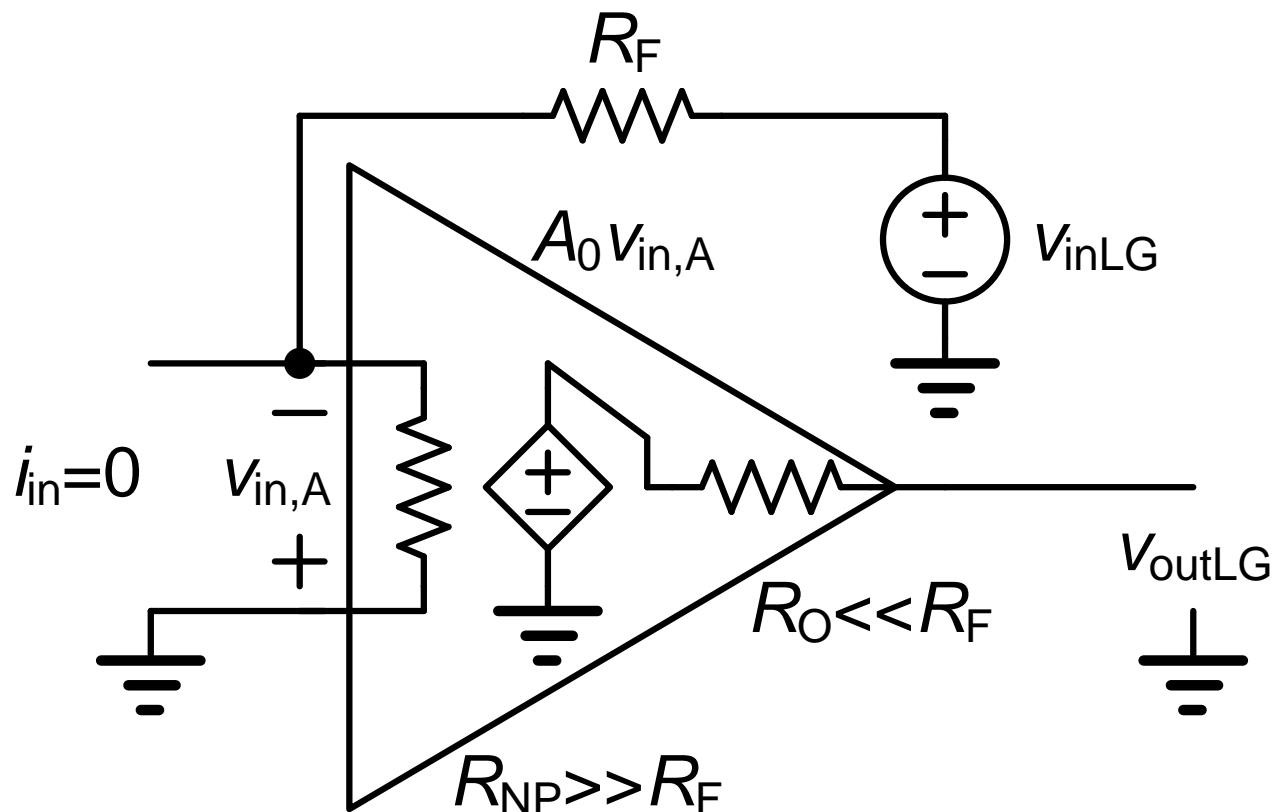
- 低噪声和高频的跨阻放大器

并联-并联反馈结构



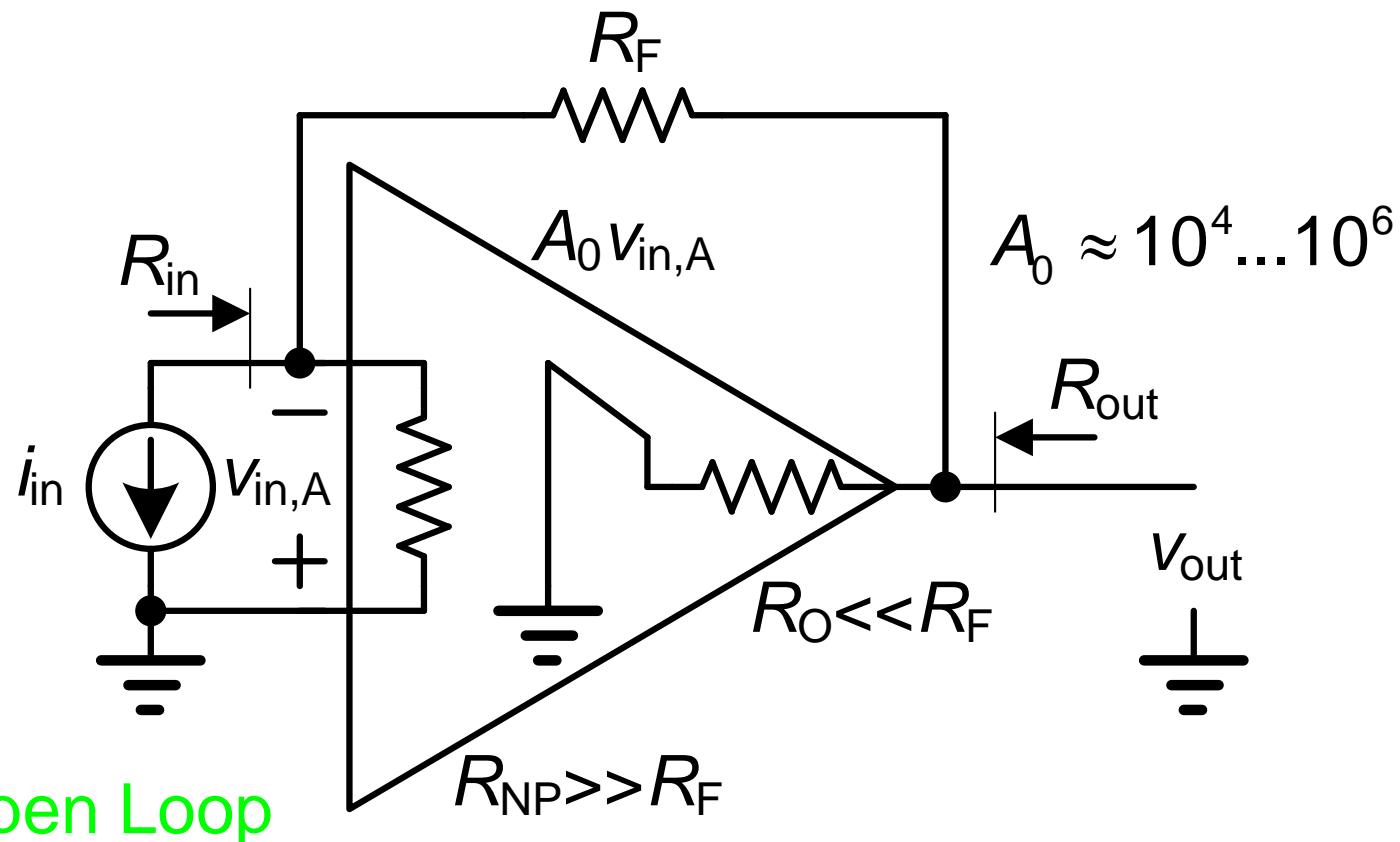
$$A_R = \frac{V_{out}}{i_{in}} = R_F \quad R_{in} \approx 0 \quad R_{out} \approx 0$$

并联-并联反馈：环路增益



$$LG = \frac{V_{outLG}}{V_{inLG}} \approx A_{VOL} \approx A_0 \approx 10^4 \dots 10^6$$

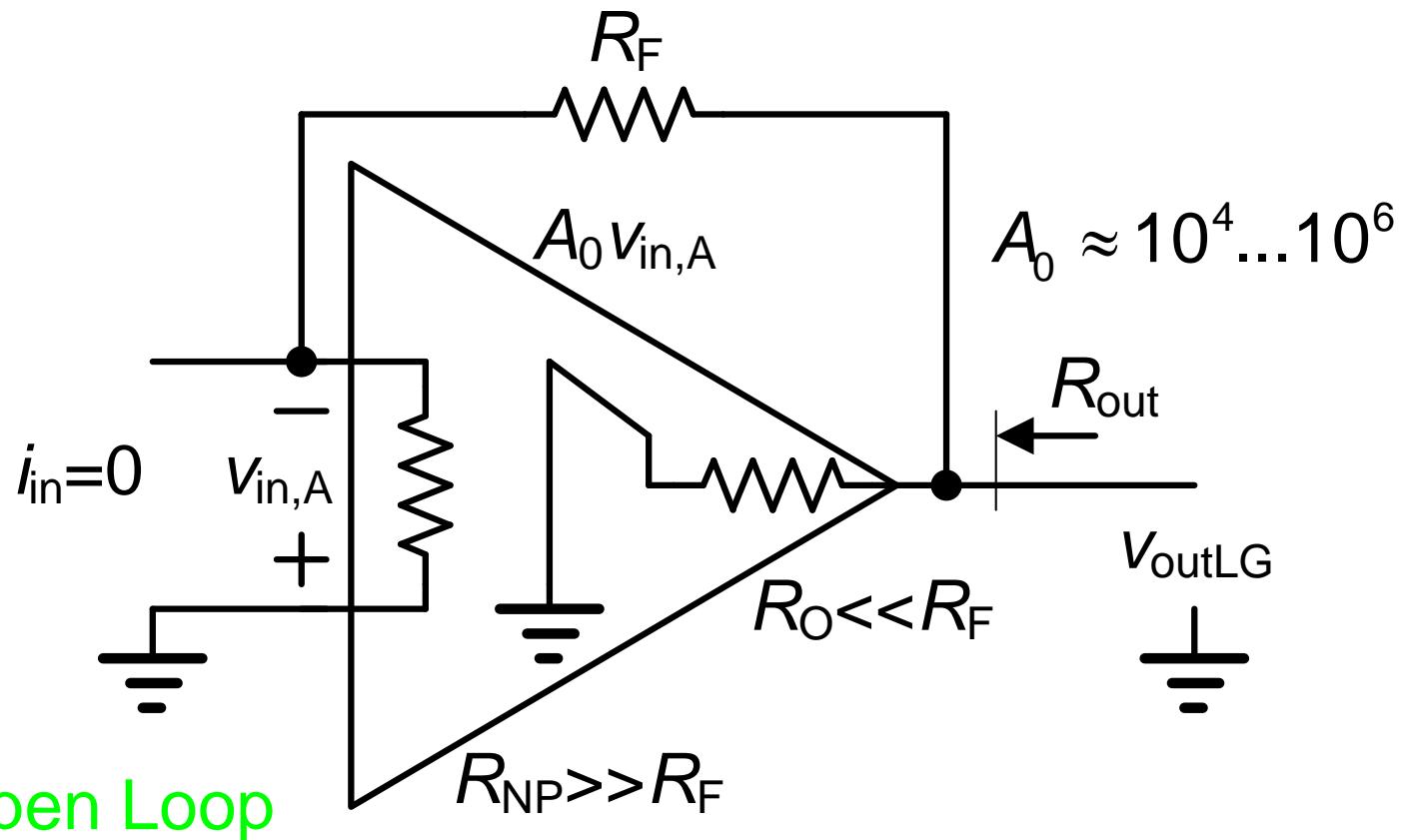
并联-并联反馈：输入电阻



$$R_{in} = \frac{V_{in}}{i_{in}} = \frac{R_{inOL}}{LG} \approx 0$$

$$\begin{aligned} R_{inOL} &= R_{in}(A_v = 0) = R_{NP} // (R_F + R_O) \\ &\approx R_F \end{aligned}$$

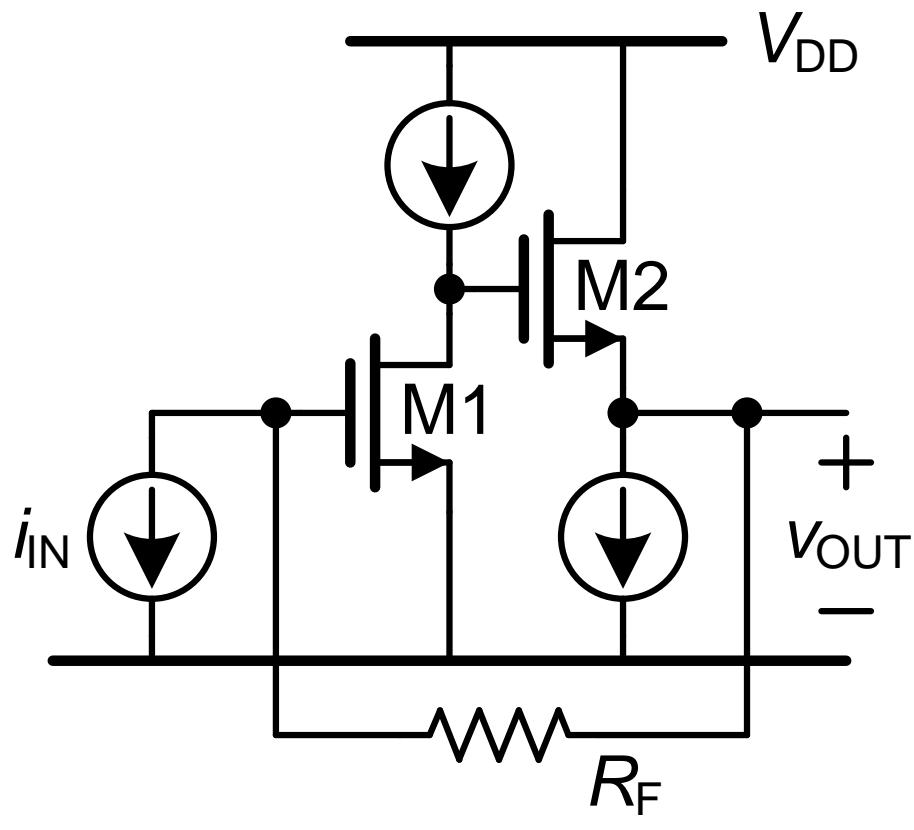
并联-并联反馈：输出电阻



$$R_{out} = \frac{R_{outOL}}{LG} \approx 0$$

$$R_{outOL} = R_{out}(A_v = 0) = R_O // (R_F + R_{NP}) \\ \approx R_O$$

并联-并联反馈



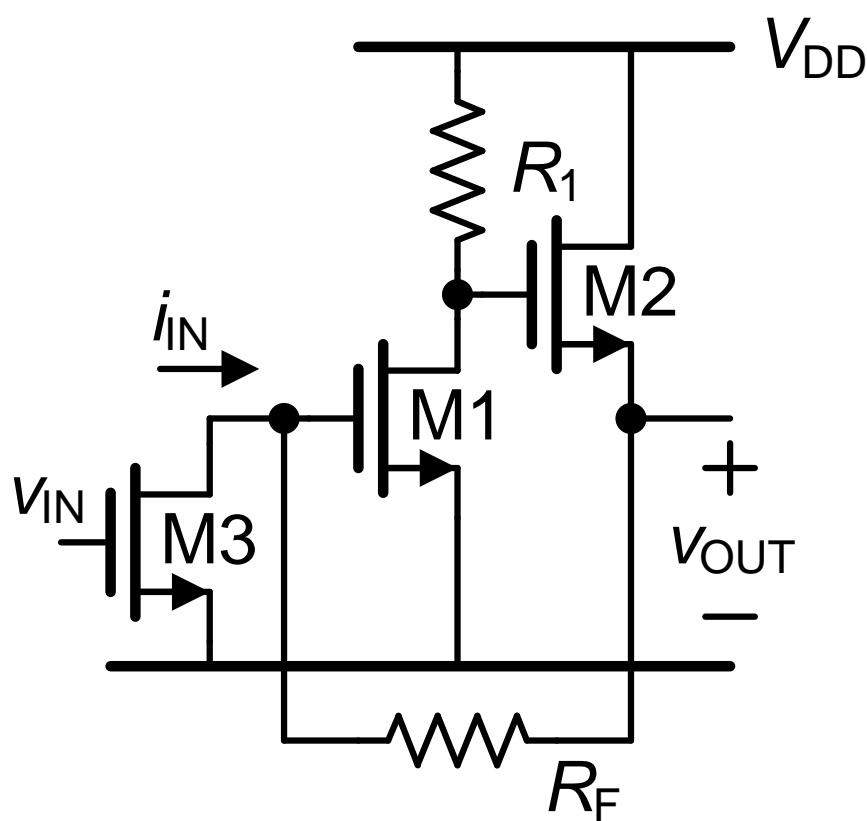
$$A_R = \frac{V_{out}}{i_{in}} = R_F$$

$$LG = g_{m1} r_{DS1}$$

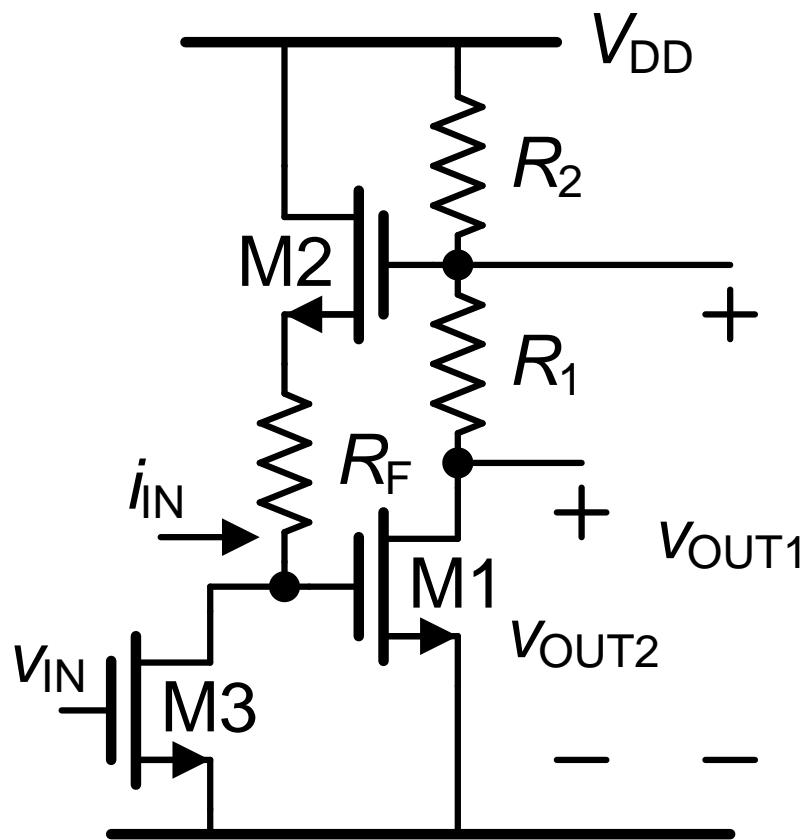
$$R_{in} = \frac{R_F}{LG} \approx 0 ?$$

$$R_{out} = \frac{1/g_{m2}}{LG} \approx 0$$

接电阻的并联-并联反馈



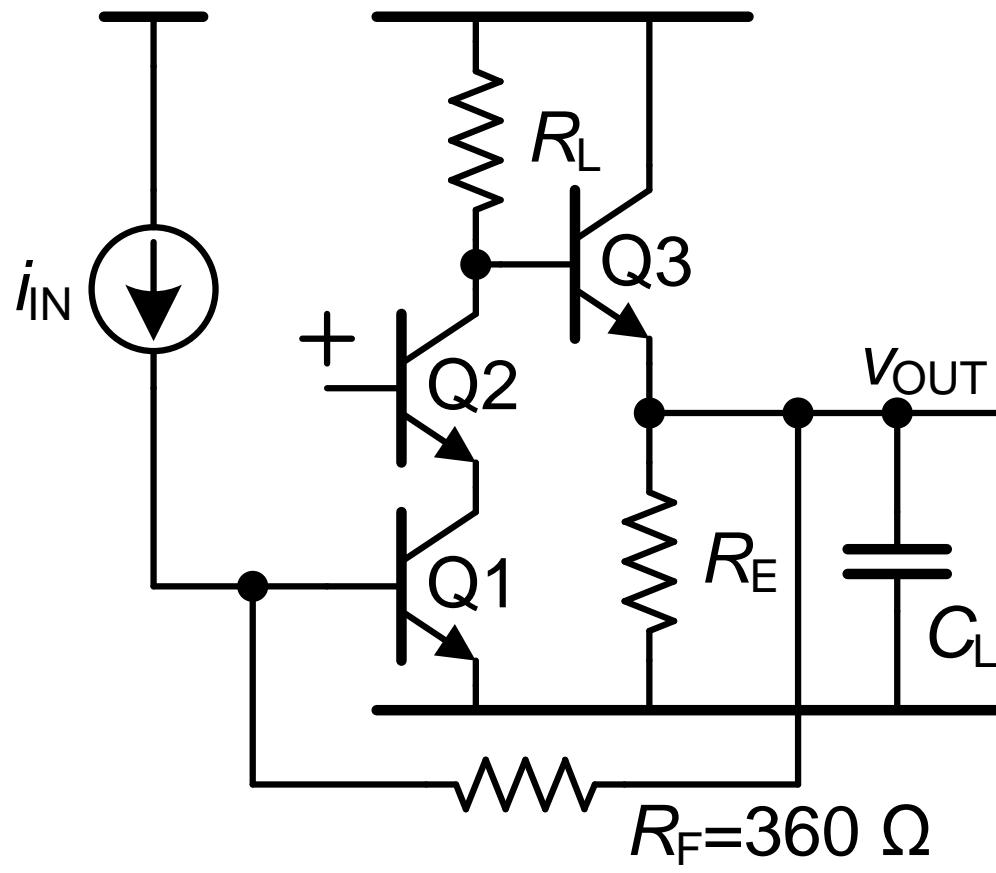
$$A_R = \frac{V_{out}}{i_{in}} = R_F$$



$$A_{R1} = R_F \quad A_{R2} = R_F \frac{R_1 + R_2}{R_2}$$

Ref.: Cherry, Proc. IEE, Feb.63, 375-389; Holdenried, JSSC Nov.04, 1959-1967

接电压放大器的电流检测器



$$f_T = 40 \text{ GHz}$$

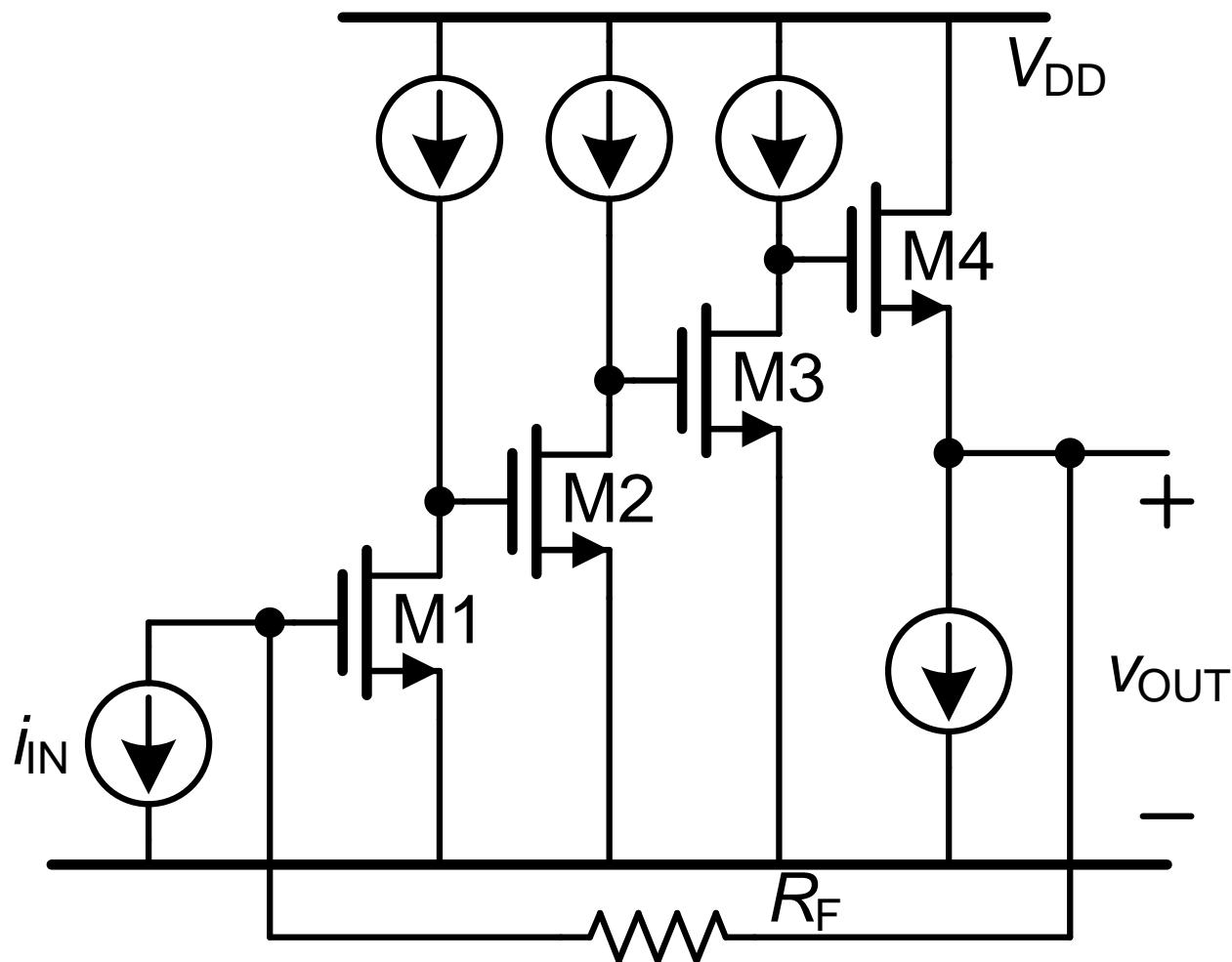
$$r_B = 20 \Omega$$

$$BW = 10 \text{ GHz}$$

$$I_{TOT} = 10 \text{ mA}$$

Ref.: Baureis, JSSC June 1993, 701-706

并联-并联反馈



$$A_R = R_F$$

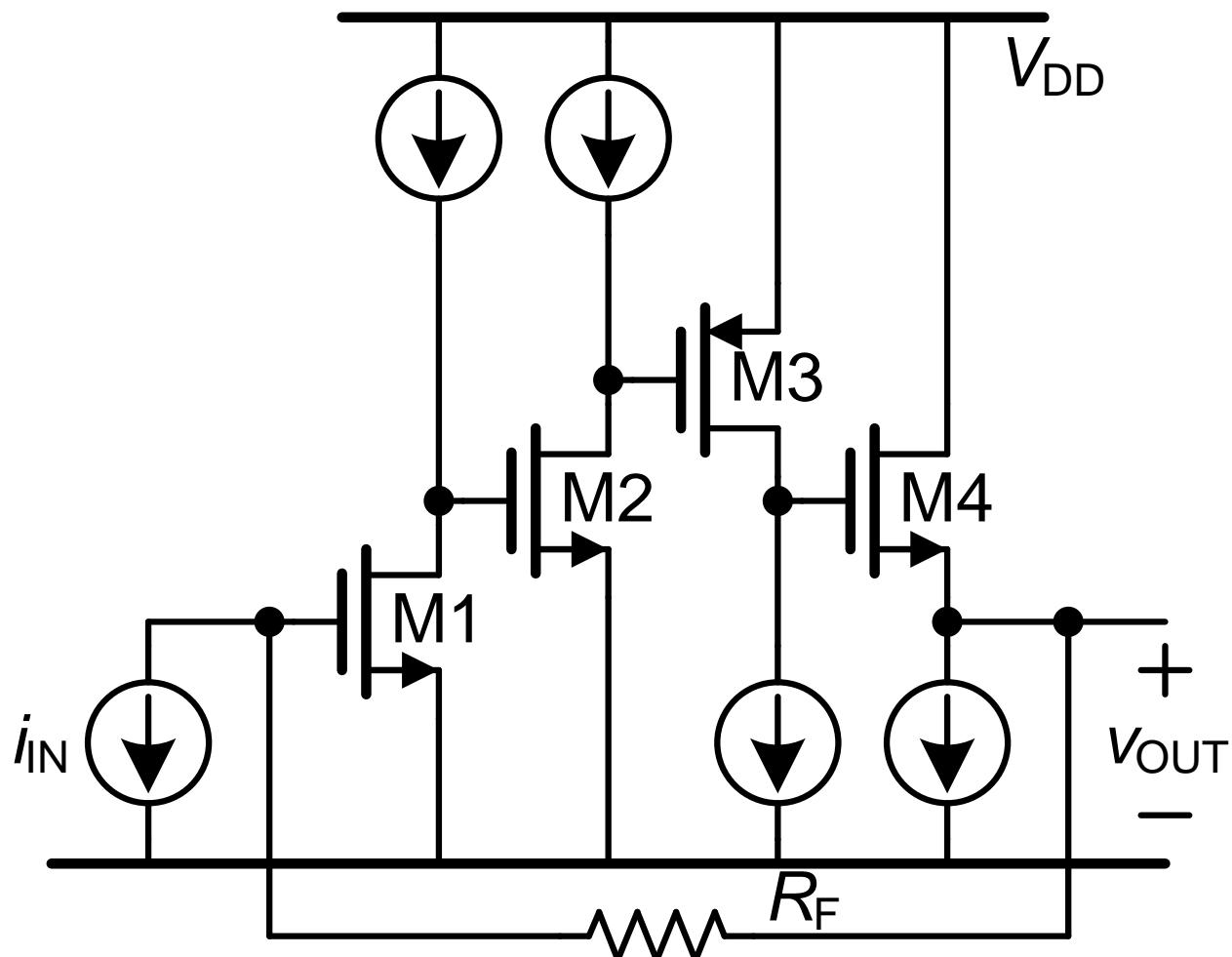
$$LG = A_{V1} A_{V2} A_{V3}$$

$$A_{Vi} = g_{mi} r_{DSi}$$

$$R_{in} = \frac{R_F}{LG} \approx 0$$

$$R_{out} = \frac{1/g_{m4}}{LG} \approx 0$$

并联-并联反馈：合理偏置



$$A_R = R_F$$

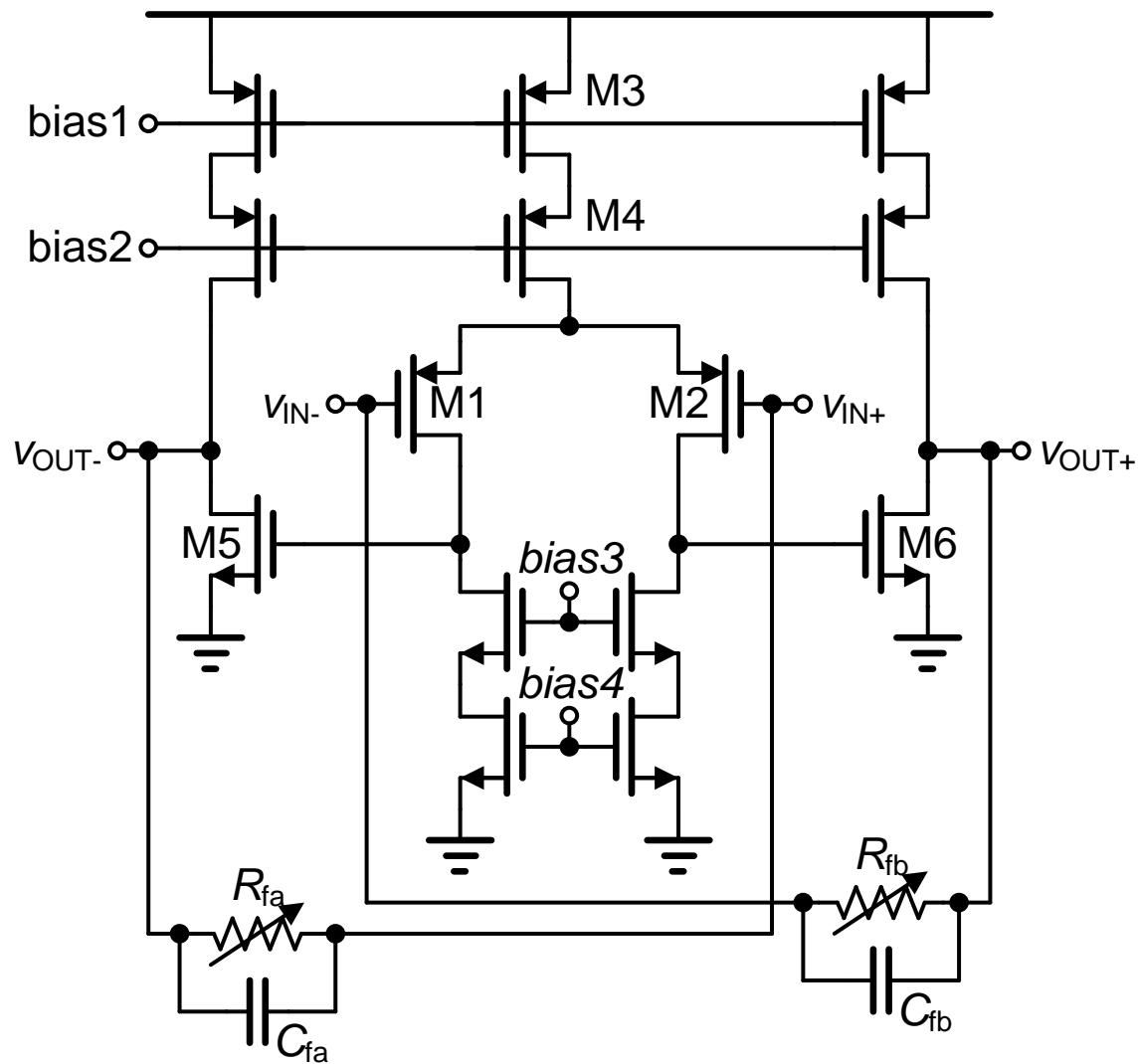
$$LG = A_{V1} A_{V2} A_{V3}$$

$$A_{Vi} = g_{mi} r_{DSi}$$

$$R_{in} = \frac{R_F}{LG} \approx 0$$

$$R_{out} = \frac{1/g_{m4}}{LG} \approx 0$$

用于光通信的CMOS前置放大器



如果为全差分，
只需两级！

20 K Ω ... 500 Ω
of R_1 & R_f

Ref.: Phang, Johns, CAS-II July 1999

差分并联-并联反馈

$$A_R = R_F$$

$$LG = A_{V1} A_{V2}$$

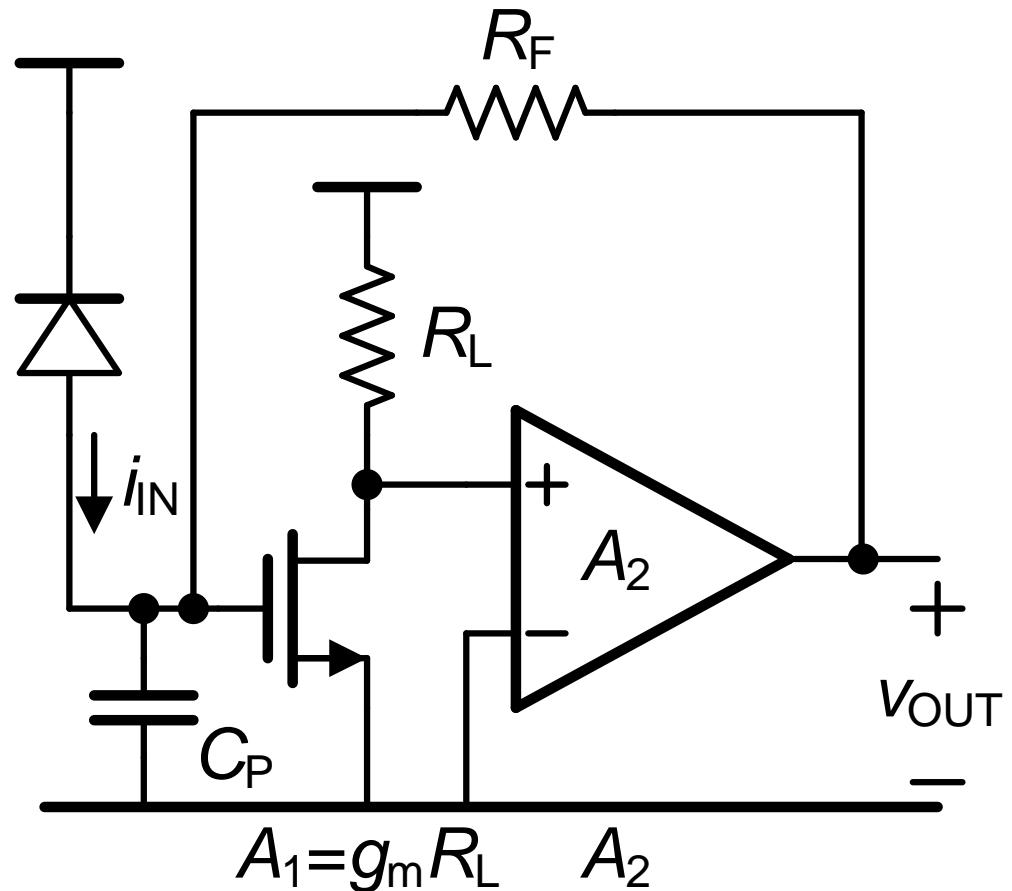
$$A_{V1} = g_{m1} r_{DS1}$$

$$A_{V2} = g_{m2} r_{DS2}$$

$$R_{in} = \frac{2R_F}{LG} \approx 0$$

$$R_{out} = \frac{2/g_{m3}}{LG} \approx 0$$

接电压放大器的电流检测器



$$R_{in} = \frac{V_{in}}{i_{in}} = \frac{R_F}{A_1 A_2}$$

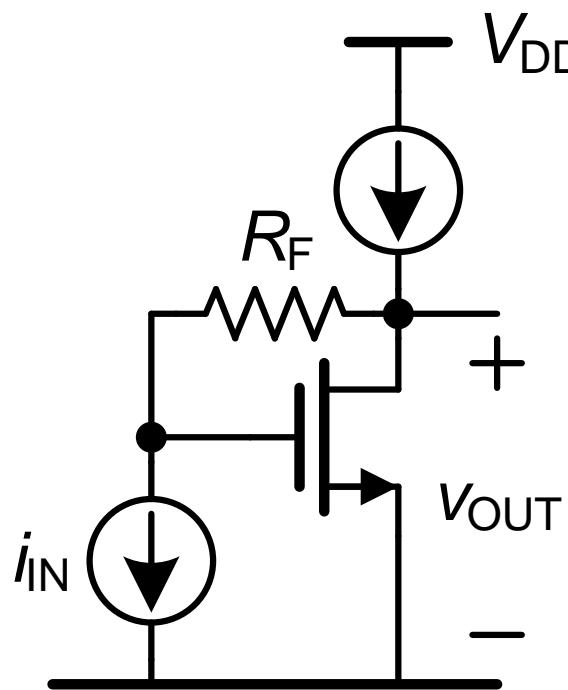
$$A_R = \frac{V_{out}}{i_{in}} = R_F$$

$$LG = A_1 A_2$$

$$f_{-3dB} = \frac{1}{2\pi R_{in} C_p}$$

Ref.: Cherry, Proc. IEE, Feb.63, 375-389

接并联-并联反馈的单管电路



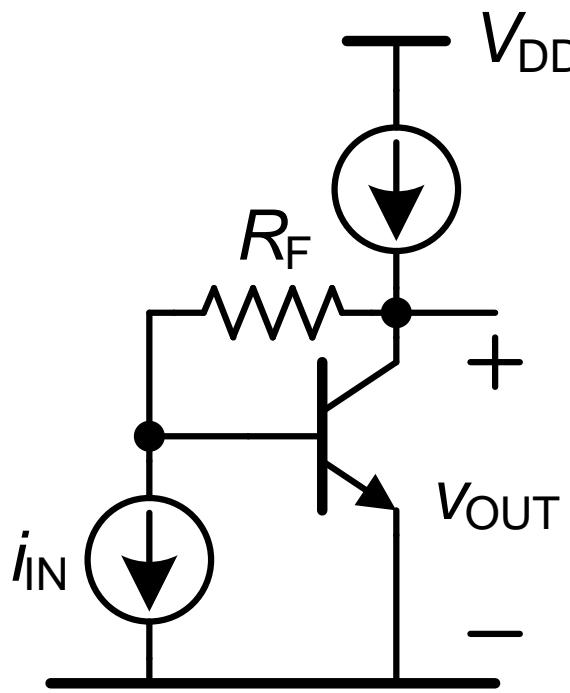
$$A_R = R_F \left(\text{if } \gg 1/g_m \right)$$

$$LG = g_m r_{DS}$$

$$R_{in} = \frac{R_F + r_{DS}}{LG} \approx 0 ?$$

$$R_{out} = \frac{r_{DS}}{LG} \approx 0 ?$$

接并联-并联反馈的单双极性晶体管



$$A_R = R_F \left(\text{if } R_F \gg g_m \right)$$

$$LG = \frac{g_m r_o r_\pi}{r_o + R_F + r_\pi}$$

$$R_{in} = \frac{(R_F + r_o) // r_\pi}{LG} \approx 0 ?$$

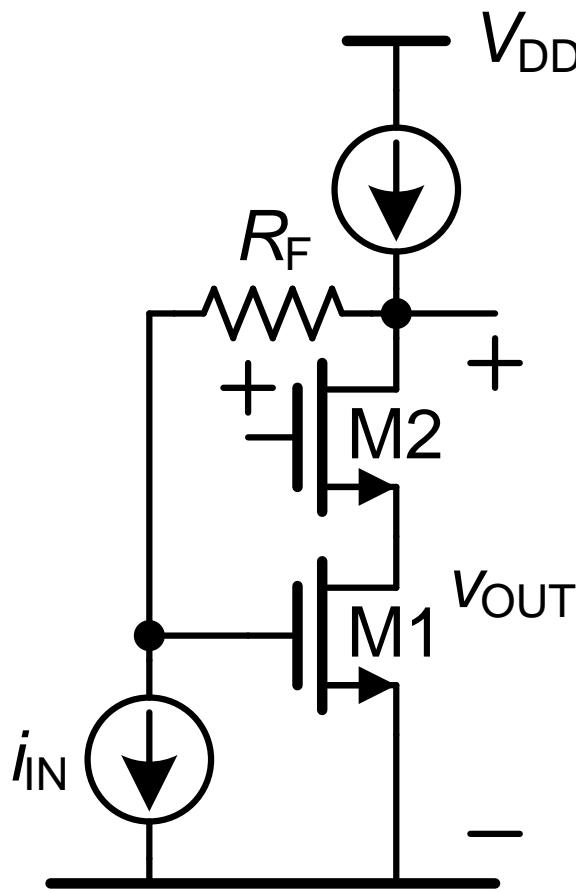
$$R_{out} = \frac{(R_F + r_\pi) // r_o}{LG} \approx 0 ?$$

远非理想 !!

输出负载效应: $R_F + r_\pi \approx r_o$

降低了 LG !!

共源共栅的并联-并联反馈



$$A_R = R_F$$

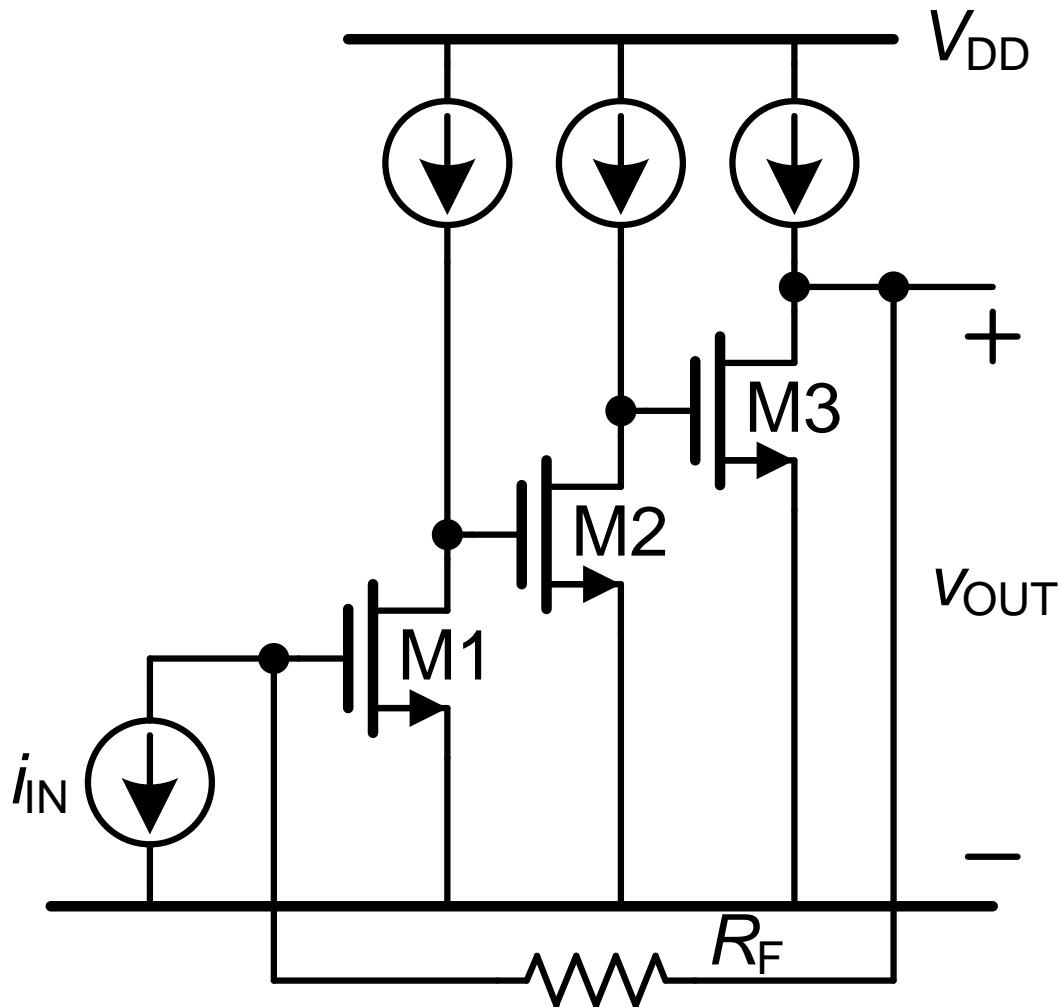
$$LG = g_{m1} r_{DS1} g_{m2} r_{DS2}$$

$$R_{in} = \frac{R_F + r_{out}}{LG} \approx \frac{1}{g_{m1}} \approx 0$$

$$r_{out} = r_{DS1} g_{m2} r_{DS2}$$

$$R_{out} = \frac{r_{out}}{LG} \approx \frac{1}{g_{m1}} \approx 0$$

MOS管并联-并联反馈



$$A_R = R_F$$

$$LG = A_{V1} A_{V2} A_{V3}$$

$$A_{Vi} = g_{mi} r_{DSi}$$

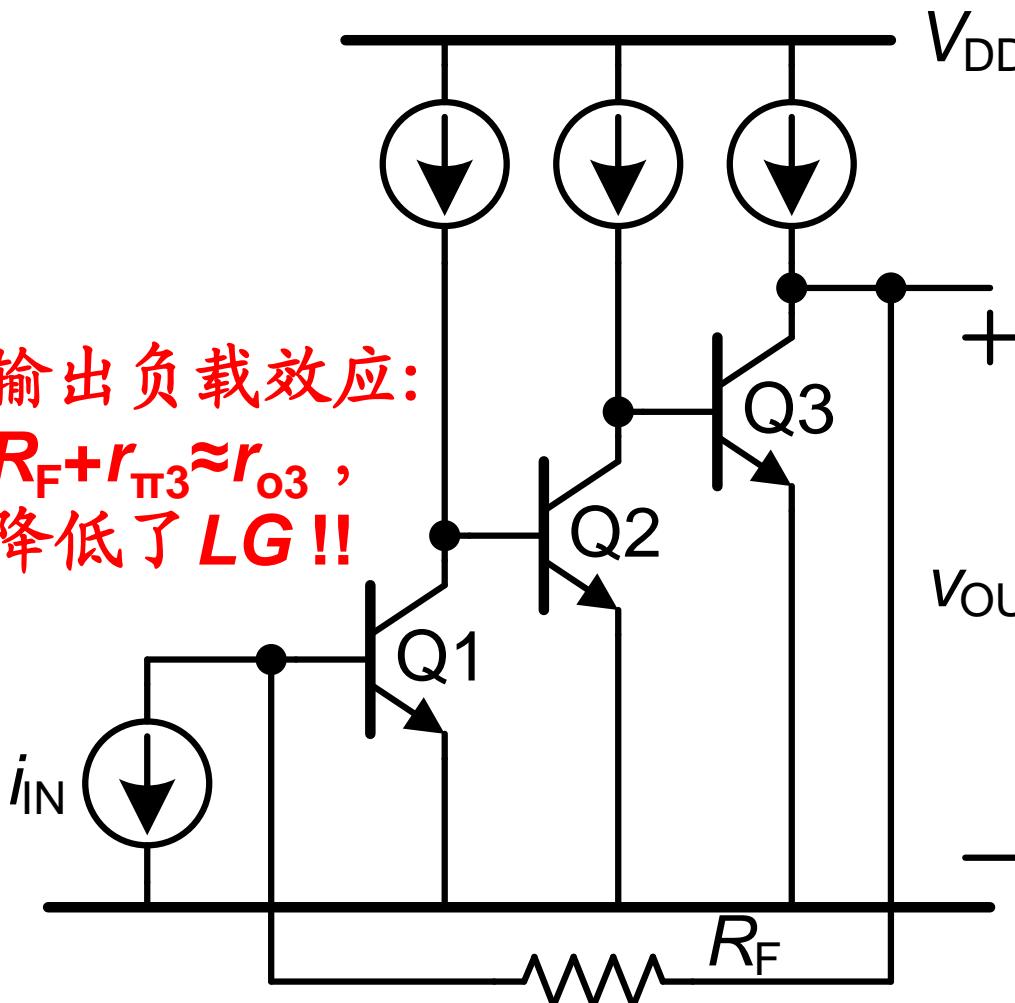
$$R_{in} = \frac{R_F + r_{DS3}}{LG} \approx 0$$

$$R_{out} = \frac{r_{DS3}}{LG} \approx 0$$

单双极性晶体管并联-并联反馈

输出负载效应:

$R_F + r_{\pi3} \approx r_{o3}$,
降低了 LG !!



$$A_R = R_F$$

$$LG = A_{V1} A_{V2} A_{V3} \frac{r_{\pi1}}{R_F + r_{\pi1}}$$

$$A_{V1} = g_{m1} (r_{o1} // r_{\pi2})$$

$$A_{V2} = g_{m2} (r_{o2} // r_{\pi3})$$

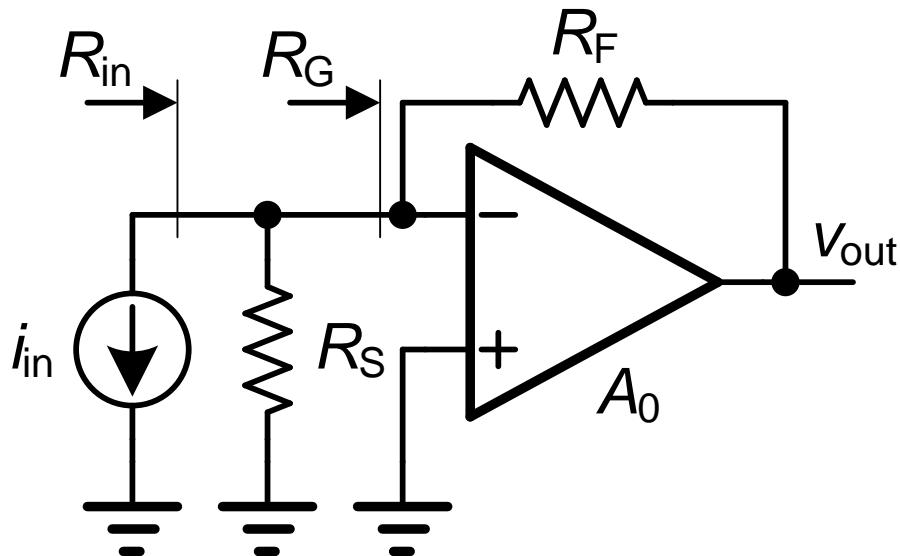
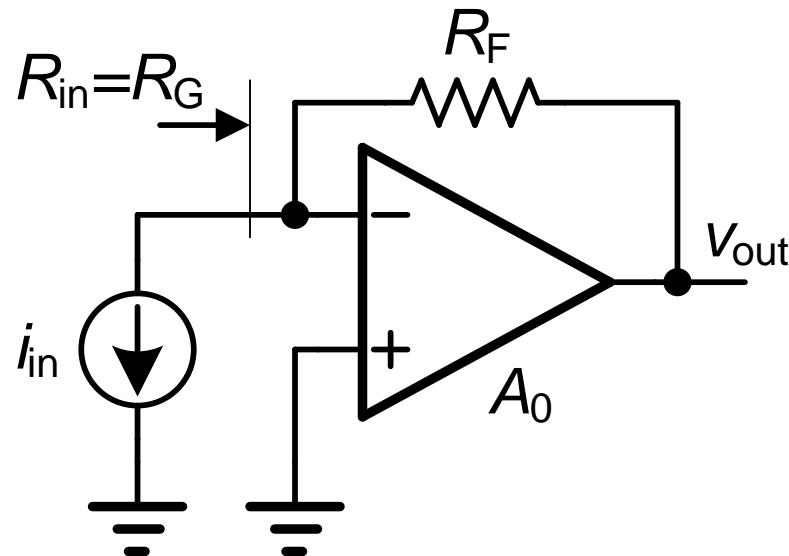
$$A_{V3} = g_{m3} R_{outOL}$$

$$R_{outOL} = r_{o3} // (R_F + r_{\pi1})$$

$$R_{out} = \frac{R_{outOL}}{LG} \approx 0$$

$$R_{in} = \frac{(R_F + r_{o3}) // r_{\pi1}}{LG} \approx 0$$

接非理想电流源的并联-并联反馈



$$A_R = R_F$$

$$LG = A_0$$

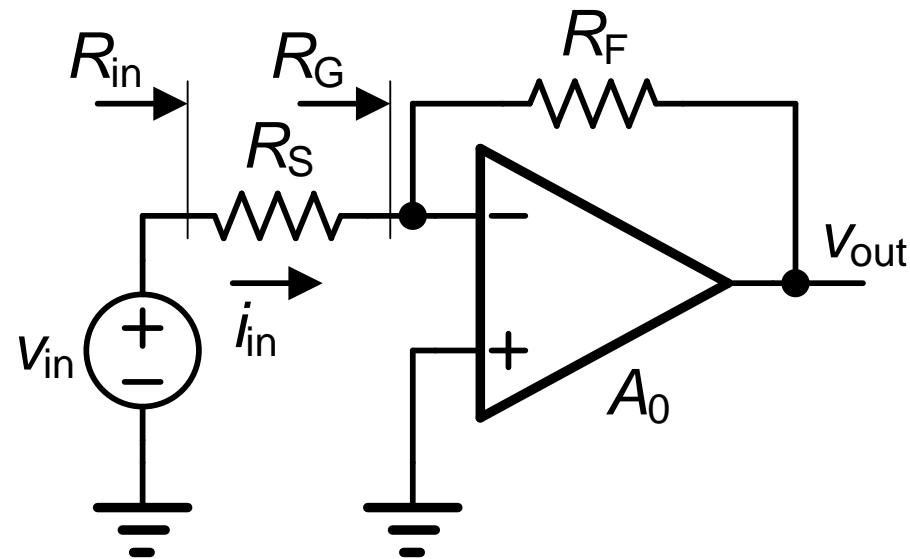
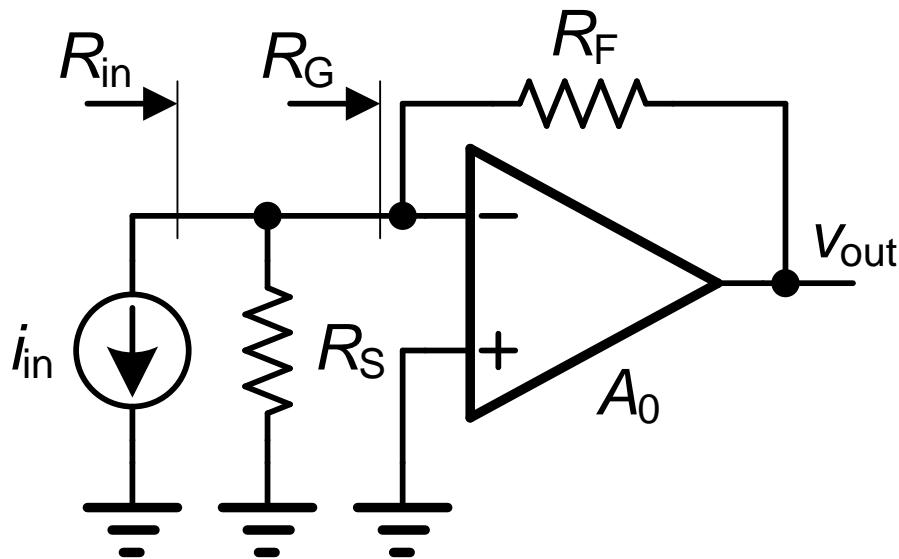
$$R_{in} = \frac{R_F}{A_0}$$

$$A_R = R_F \quad \text{if } R_S > \frac{R_F}{A_0}$$

$$LG = A_0$$

$$R_G = \frac{R_F}{A_0} \quad R_{in} = R_G // R_S$$

接电压源的并联-并联反馈



$$A_R = R_F \quad \text{if } R_S > \frac{R_F}{A_0}$$

$$LG = A_0$$

$$R_G = \frac{R_F}{A_0} \quad R_{in} = R_G // R_S$$

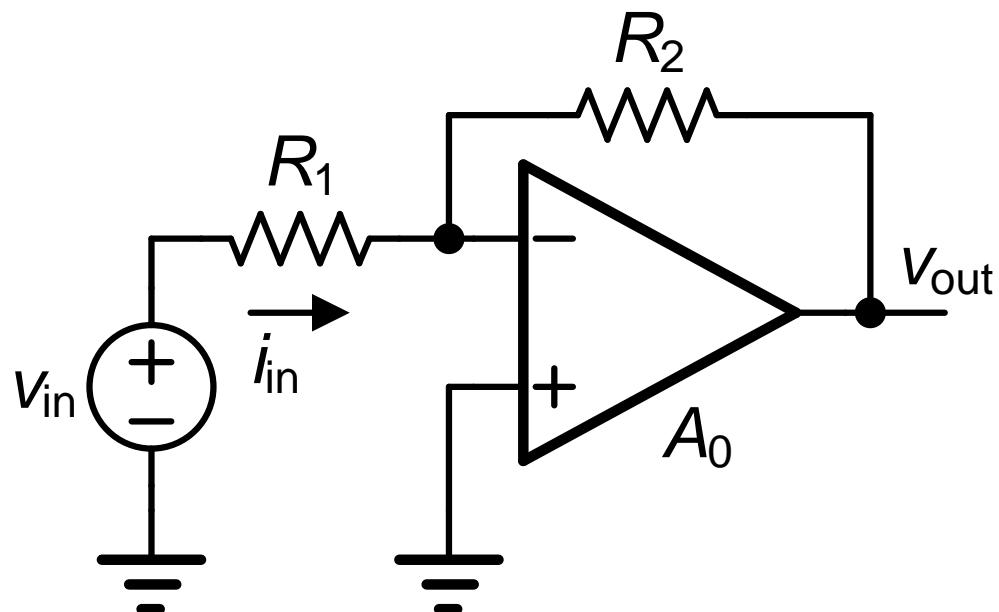
$$A_R = R_F \quad \text{if } R_S > \frac{R_F}{A_0}$$

$$LG = A_0$$

$$R_G = \frac{R_F}{A_0} \quad R_{in} = R_G + R_S$$

并联-并联反馈：增益和输出电阻

$$LG = A_0 \quad A_0 \approx 10^4 \dots 10^6$$



$$A_R = R_2 \text{ if } R_1 > \frac{R_2}{A_0}$$

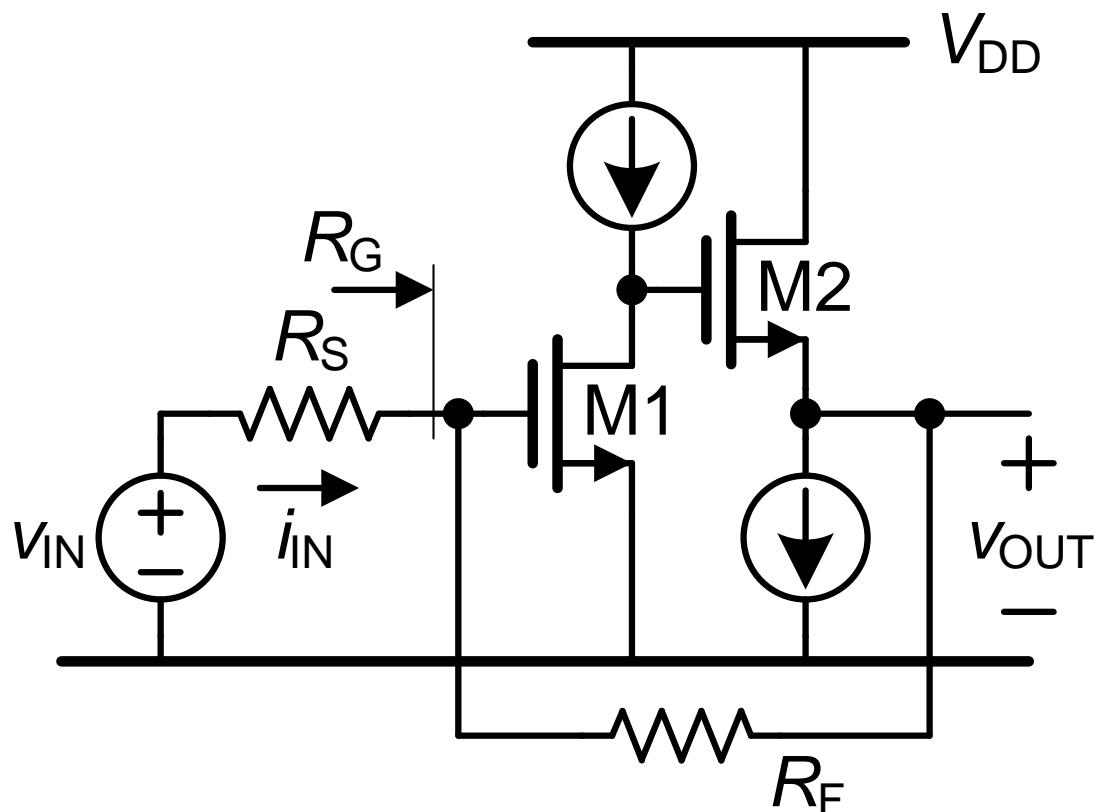
$$\frac{V_{out}}{V_{in}} = \frac{V_{out}}{i_{in}} \frac{i_{in}}{V_{in}}$$

$$A_v = -A_R \frac{1}{R_1}$$

$$= -\frac{R_2}{R_1}$$

$$R_{out} = \frac{R_{outOL}}{LG}$$

接电压源的并联-并联反馈



if $R_S > \frac{R_F}{A_0}$

$$A_R = R_F$$

$$A_V = -\frac{R_F}{R_S}$$

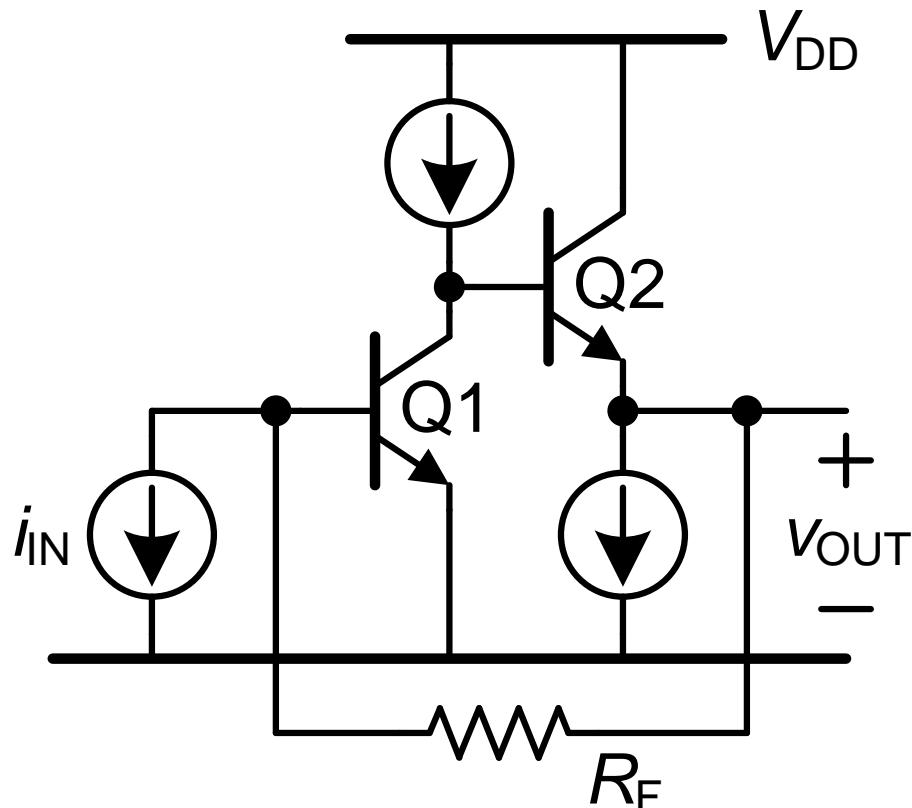
$$LG = g_{m1}r_{DS1}$$

$$R_{in} = R_S + R_G$$

$$R_G = \frac{R_F}{LG} = \frac{R_F}{g_{m1}r_{DS1}} \approx 0$$

$$R_{out} = \frac{1/g_{m2}}{LG} \approx 0$$

并联-并联反馈的输入负载效应



输入负载效应: $R_F \approx r_{\pi 1}$

$$A_R = R_F$$

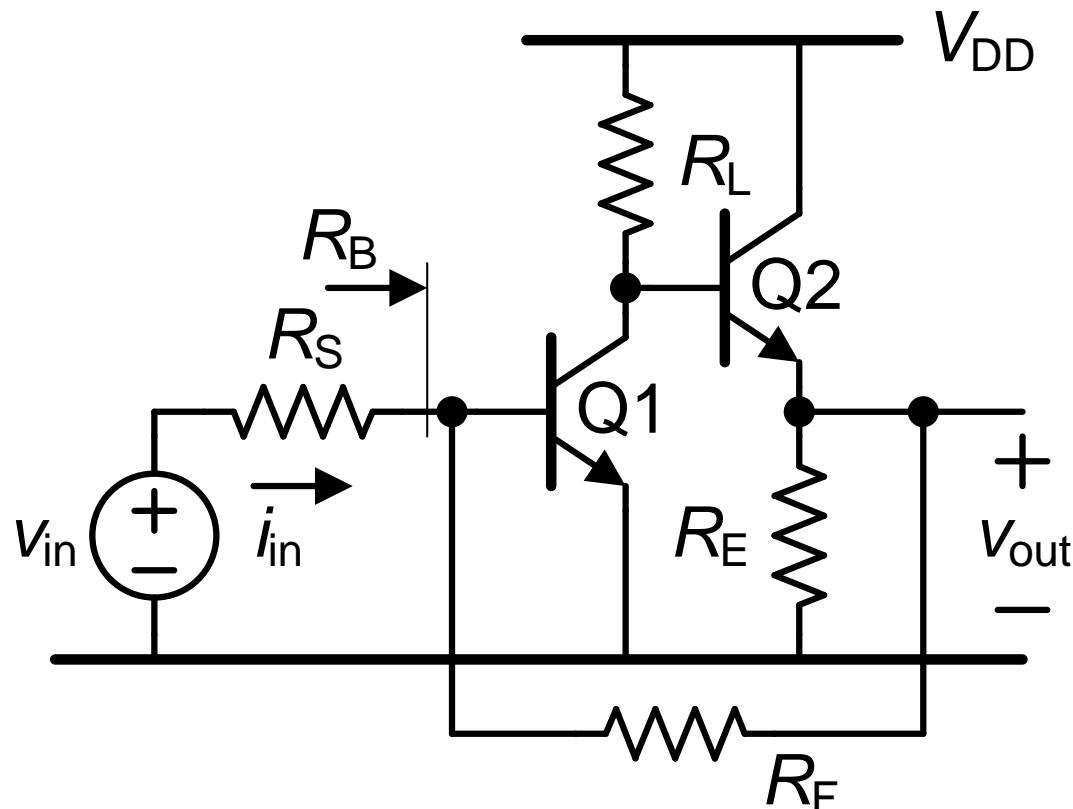
$$LG = g_{m1}r_{o1} \frac{r_{\pi 1}}{R_F + r_{\pi 1}}$$

$$R_{in} = \frac{R_F // r_{\pi 1}}{LG} = \frac{R_F}{g_{m1}r_{o1}} \approx 0$$

$$R_{out} = \frac{R_{outOL}}{LG} \approx 0$$

$$R_{outOL} = \frac{1}{g_{m2}} + \frac{r_{o1}}{\beta}$$

接电压源的并联-并联反馈



输入负载效应: $R_F \approx r_{\pi 1}$

$$R_{out} = \frac{R_{outOL}}{LG} \approx 0$$

$$A_R = R_F$$

$$A_V = -\frac{R_F}{R_S}$$

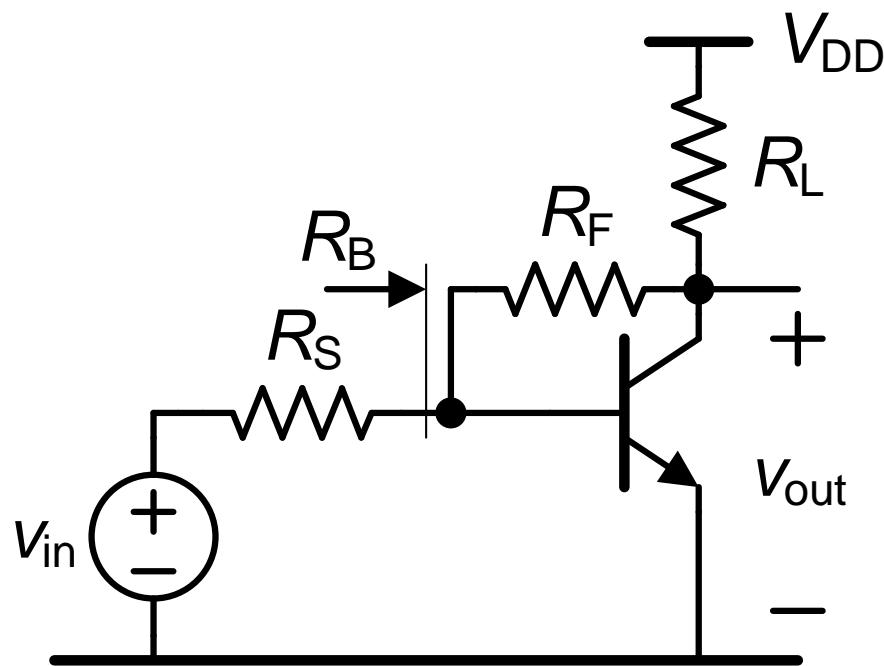
$$LG = g_{m1} R_L \frac{r_{\pi 1}}{R_F + r_{\pi 1}}$$

$$R_B = \frac{R_F // r_{\pi 1}}{LG} \approx 0$$

$$R_{in} = R_S + R_B$$

$$R_{outOL} = \frac{1}{g_{m2}} + \frac{R_L}{\beta}$$

非理想单晶体管并联-并联反馈



$$A_R \approx R_F$$

$$A_V \approx -\frac{R_F}{R_S}$$

$$LG \approx g_{m1} r_{oLF}$$

$$R_{in} = R_S + R_B$$

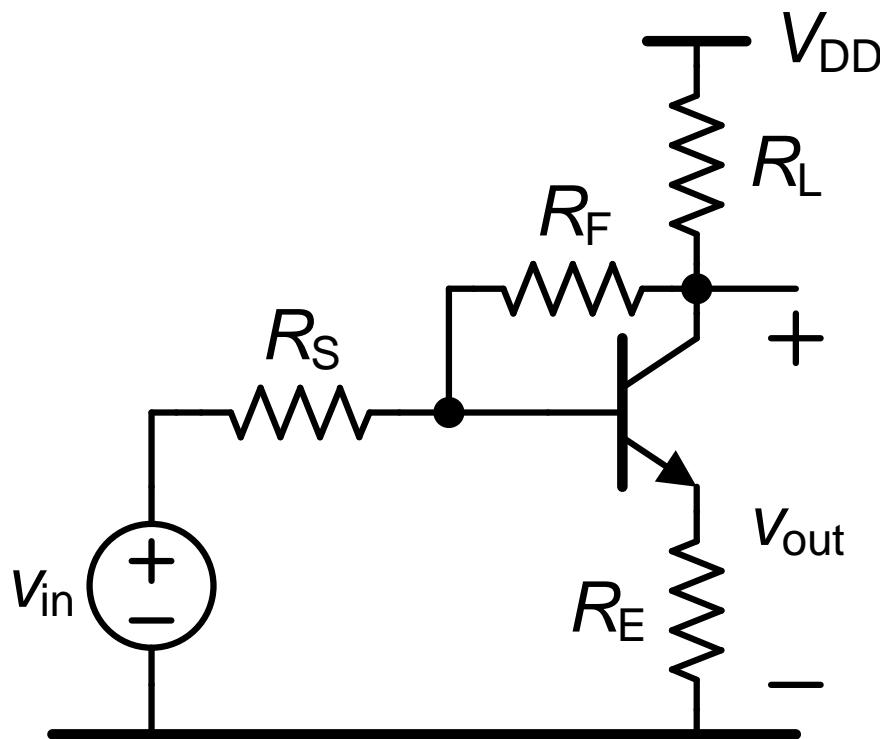
$$R_B \approx \frac{r_\pi // (R_F + r_{oL})}{LG} \approx 0$$

$$R_{out} \approx \frac{r_{oLF}}{LG} \approx 0 ??$$

输入负载效应: $R_F \approx r_{oL}$ $r_{oL} = r_o // R_L$ $r_{oLF} = r_o // R_L // R_F$

输出负载效应: $R_F \approx r_\pi$

非理想单晶体管反馈



$$A_R = R_F$$

$$A_V = -\frac{R_F}{R_S}$$

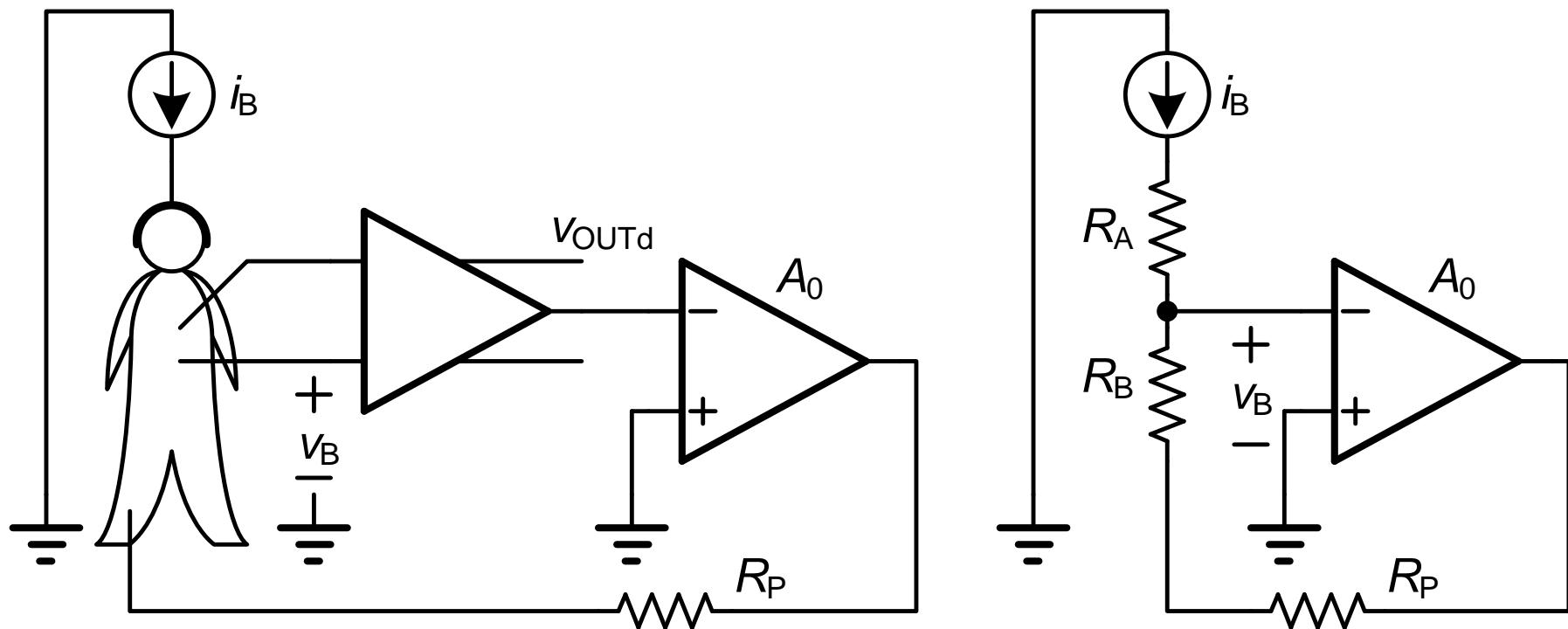
$$LG = ?$$

$$R_{in} = ?$$

$$R_{out} = ?$$

输入负载效应: $R_F \approx r_{oL}$ $r_{oL} = r_o // R_L$
 输出负载效应: $R_F \approx r_\pi$

ECG检测电路的并联-并联反馈



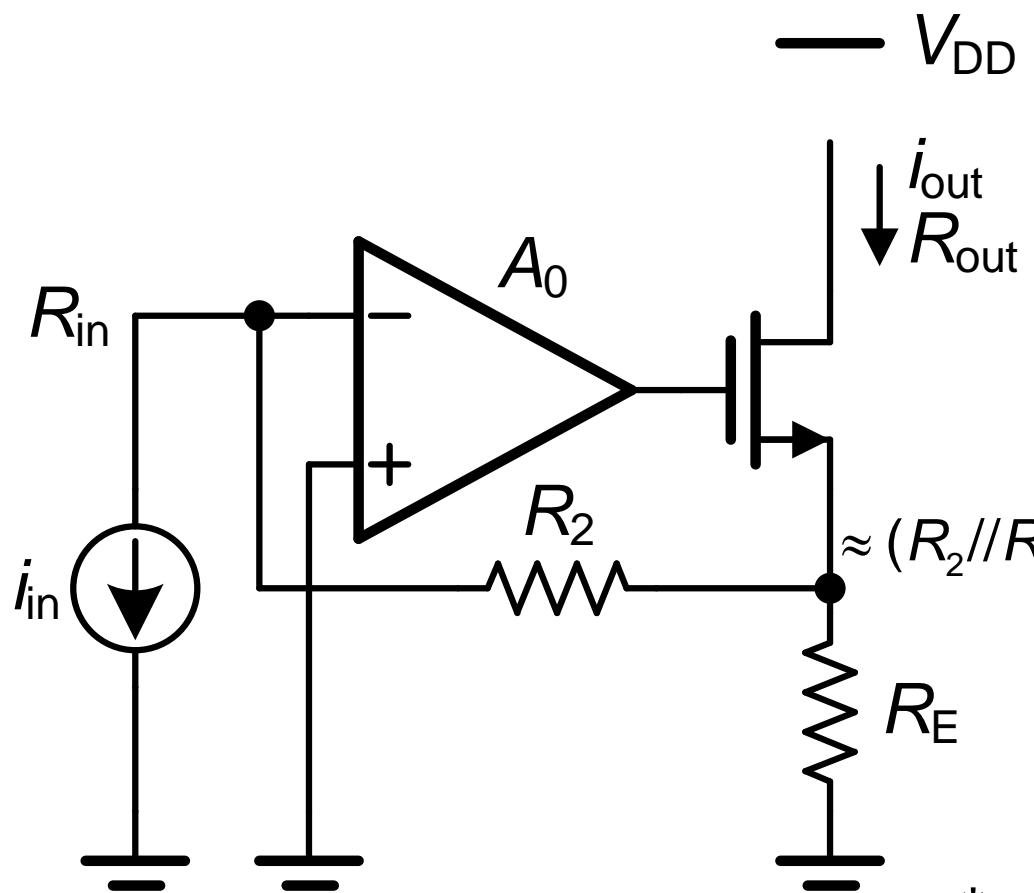
当 $220 \text{ V}_{\text{RMS}}$ (50 Hz) 经过 150 pF 的电容时
 $i_B \approx 10 \mu\text{A}_{\text{RMS}}$

$$\frac{V_B}{i_B} = \frac{R_P + R_B}{A_0 + 1}$$

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- 低噪声和高频的跨阻放大器

并联-串联反馈：增益、 R_{in} 和 R_{out}



$$LG = A_0$$

$$A = 1 + \frac{R_2}{R_E}$$

$$R_{in}^* = \frac{R_2}{LG}$$

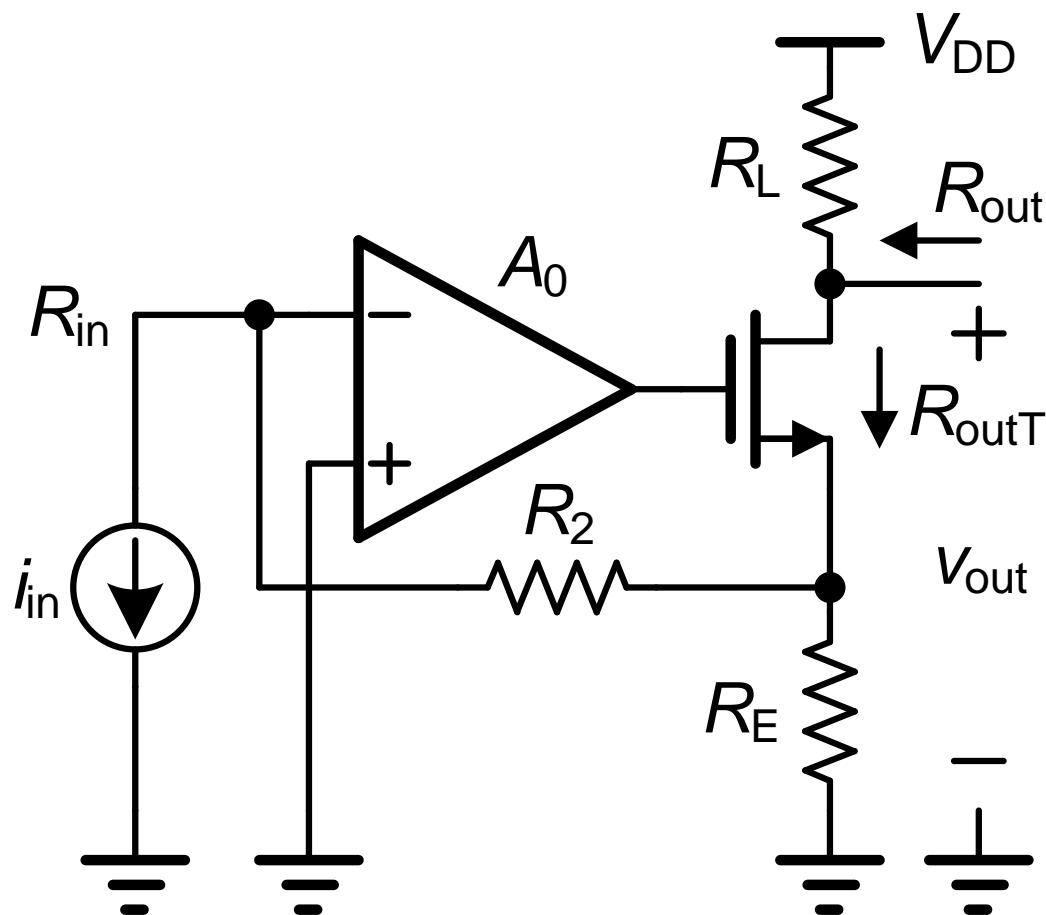
$$R_{outOL} = r_{DS}(1 + g_m R_E)$$

$$R_{out} = R_{outOL} LG \approx \infty$$

$$R_2^* = R_2 + R_E / (1 + g_m R_E) \approx R_2$$

$$R_E > 1/g_m \quad R_2 > 1/g_m$$

接负载 R_L 的并联-串联反馈



$$R_E > 1/g_m \quad R_2 > 1/g_m$$

$$R_2^* = R_2 + R_E / (1 + g_m R_E) \approx R_2$$

$$LG = A_0$$

$$A_1 = 1 + \frac{R_2}{R_E}$$

$$A_R = A R_L$$

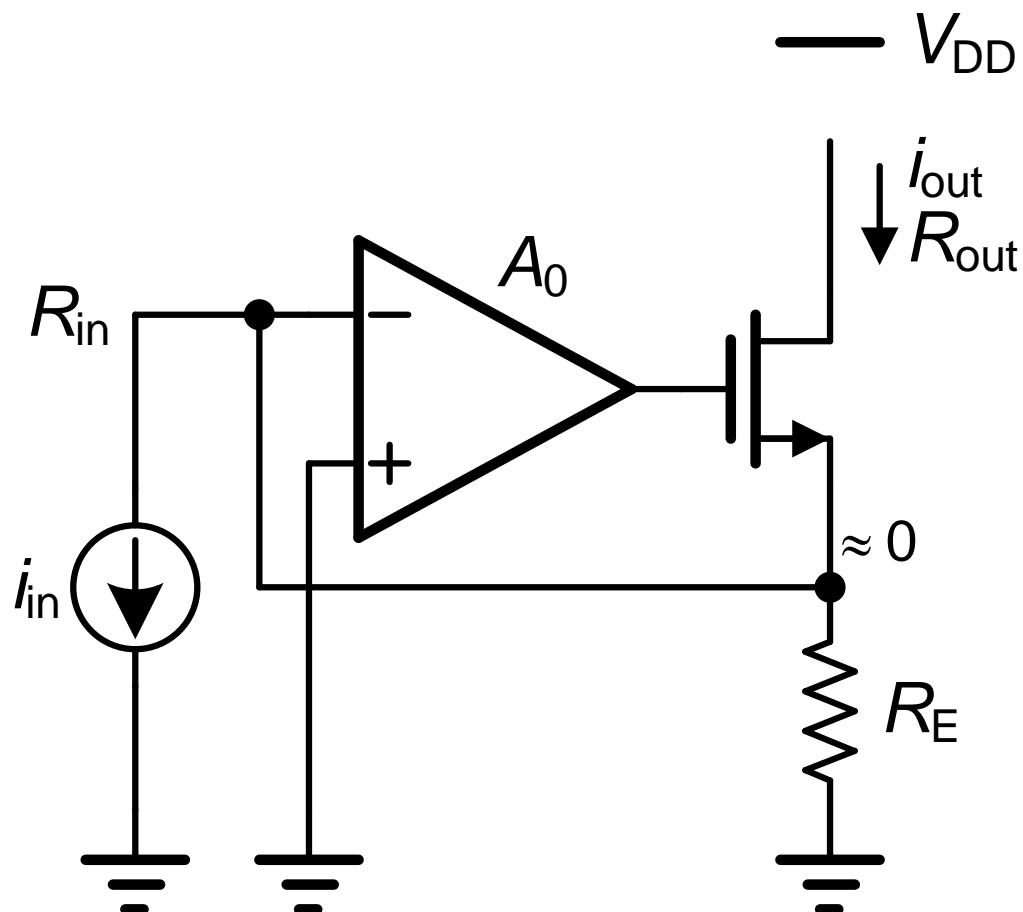
$$R_{in}^* = \frac{R_2}{LG} \approx 0$$

$$R_{out} = R_{outT} // R_L \approx R_L$$

$$R_{outT} = R_{outTOL} \quad LG \approx \infty$$

$$R_{outTOL} = r_{DS} (1 + g_m R_E)$$

理想电流缓冲器



$$A_i = 1$$

$$LG = A_0$$

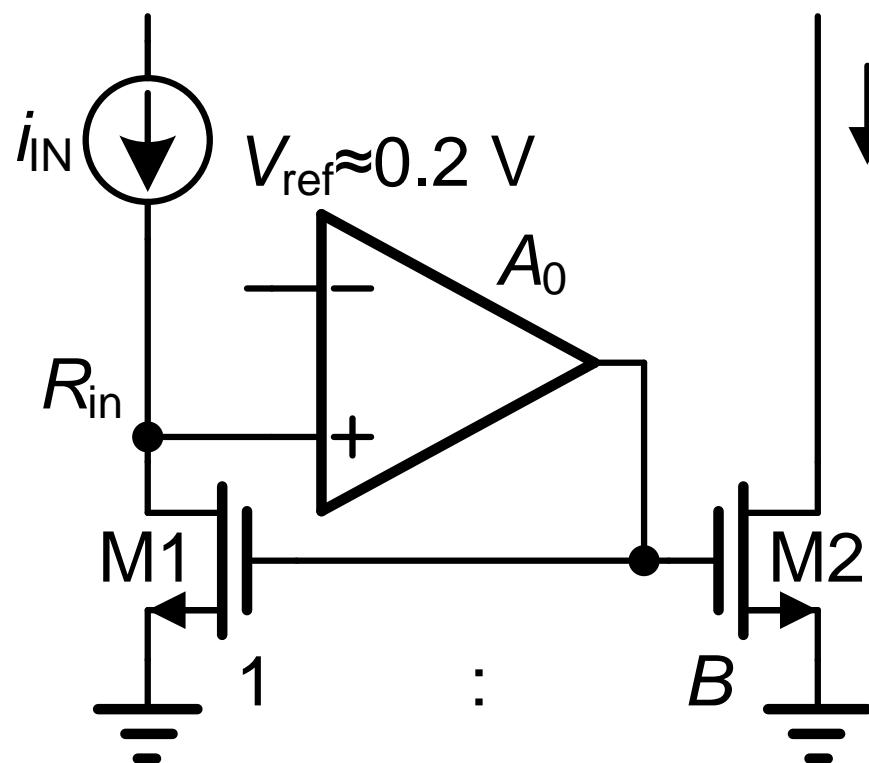
$$R_{in} = \frac{1/g_m}{LG} \approx 0$$

$$R_{outOL} = r_{DS}(1 + g_m R_E)$$

$$R_{out} = R_{outOL} LG \approx \infty$$

$$R_E > 1/g_m$$

理想电流镜



$$A_1 = B$$

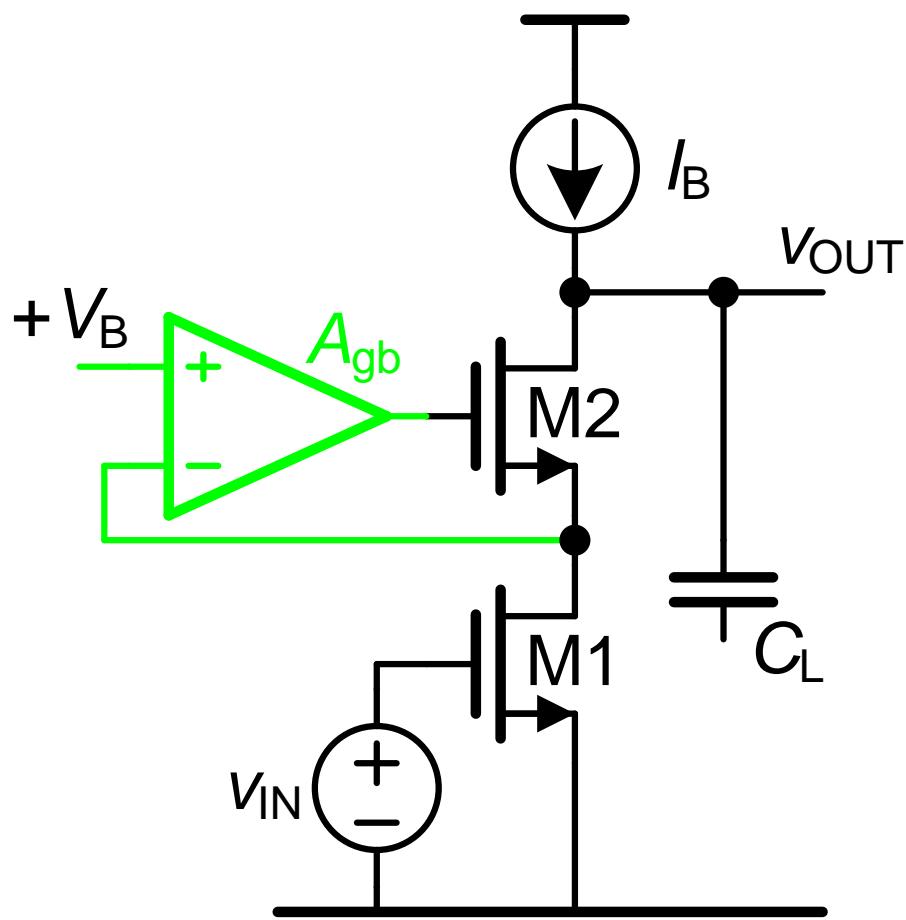
$$LG = g_{m1} r_{DS1} A_0$$

$$R_{in} = \frac{R_{inOL}}{LG} = \frac{1}{g_{m1} A_0} \approx 0$$

$$R_{inOL} = r_{DS1}$$

$$R_{out} = r_{DS2}$$

增益抬升



$$LG = A_{gb}$$

$$R_{E2} = \frac{1/g_{m2}}{LG} \approx 0$$

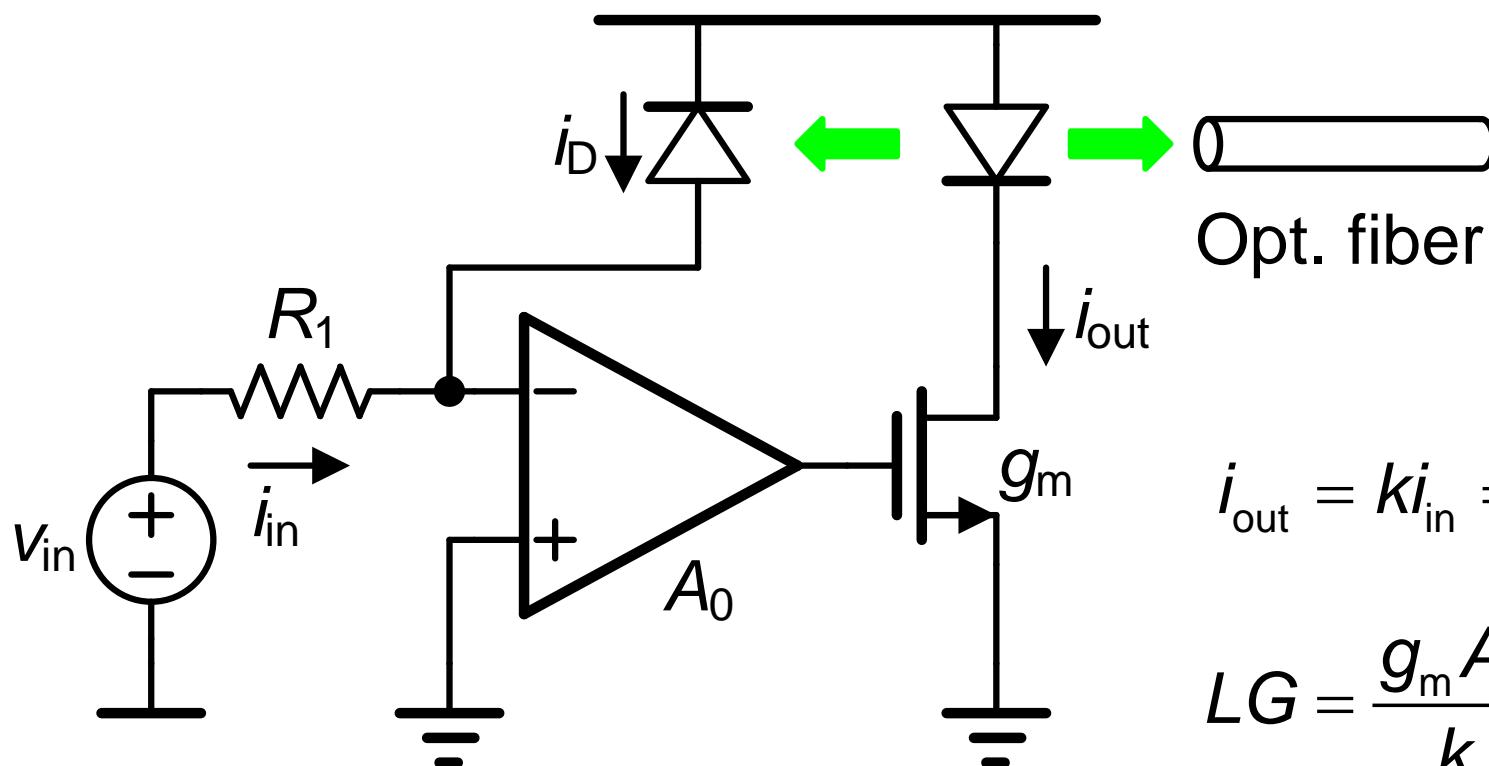
$$R_{outOL} = r_{DS2}(1 + g_{m2}r_{DS1})$$

$$R_{out} = R_{outOL} LG \approx \infty$$

$$A_v = A_{gb} (g_m r_{DS})_1 (g_m r_{DS})_2$$

Ref.: Hosticka, JSSC Dec.79, pp. 1111-1114; Sackinger, JSSC Febr.90, pp. 289-298;
 Bult JSSC Dec.90, pp. 1379-1384

线性发光二极管驱动器



$$i_{out} = k i_{in} = k \frac{V_{in}}{R_1}$$

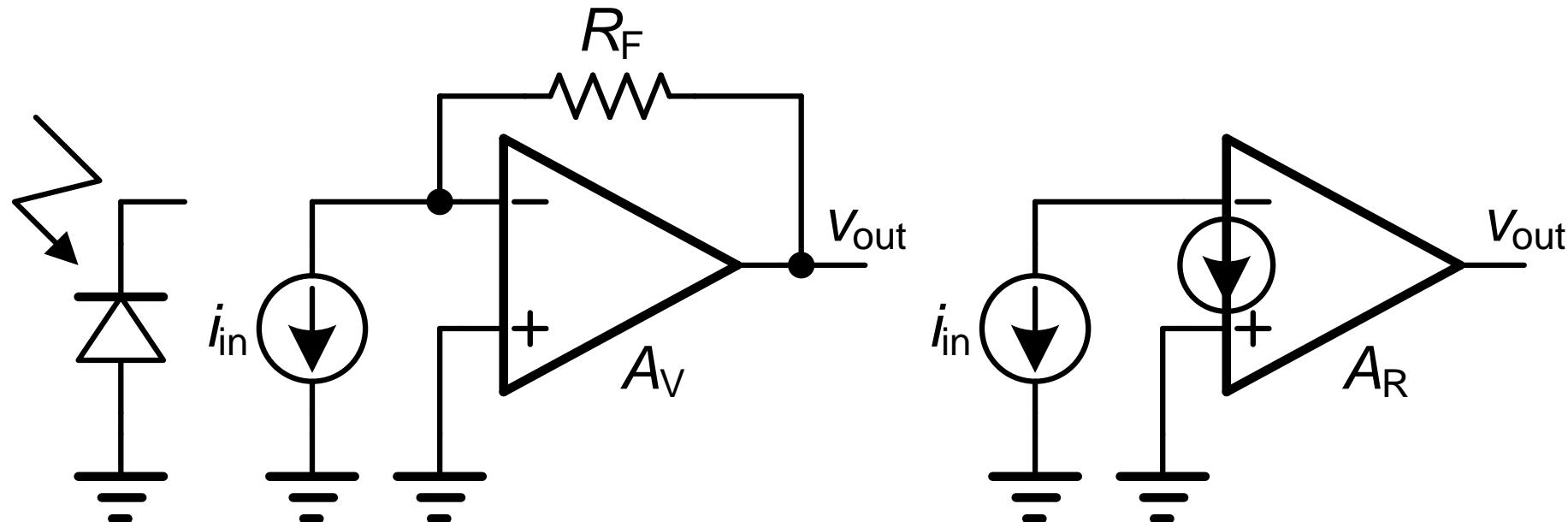
$$LG = \frac{g_m A_0}{k}$$

$$i_D = \frac{i_{out}}{k}$$

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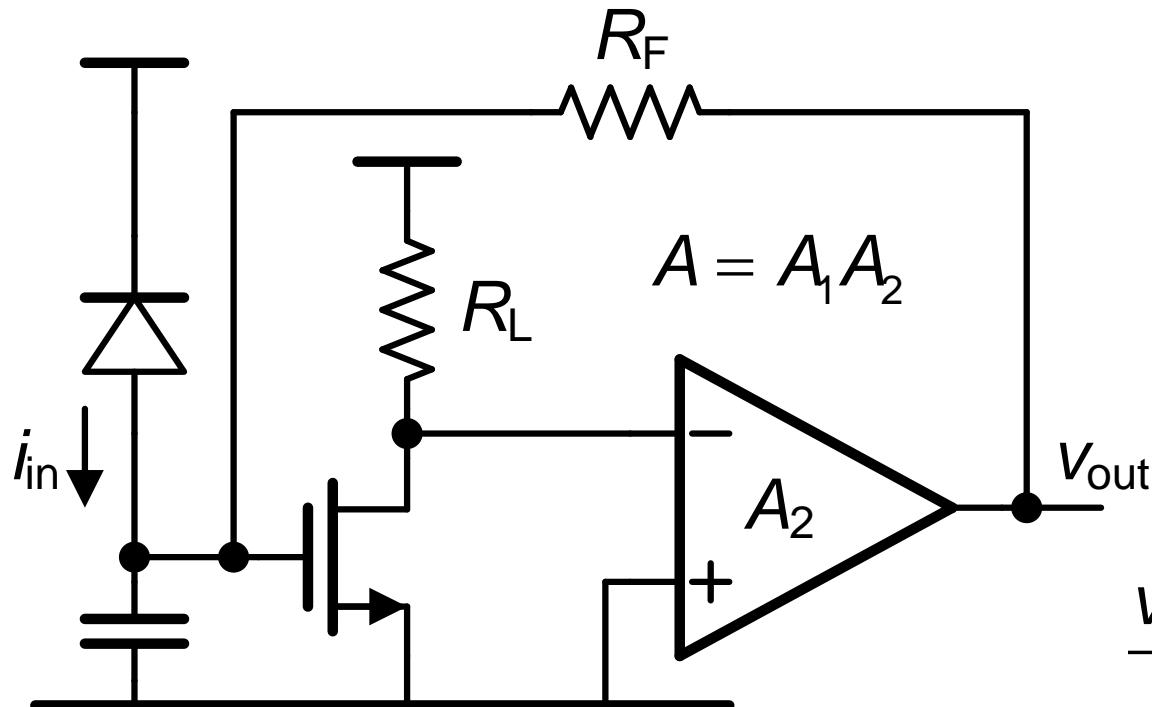
光接收器：电流或电压放大器



$$V_{out} = R_F i_{in}$$

$$V_{out} = A_R i_{in}$$

接电压放大器的电流检测器 1



噪声匹配: $C_D = C_{GS}$

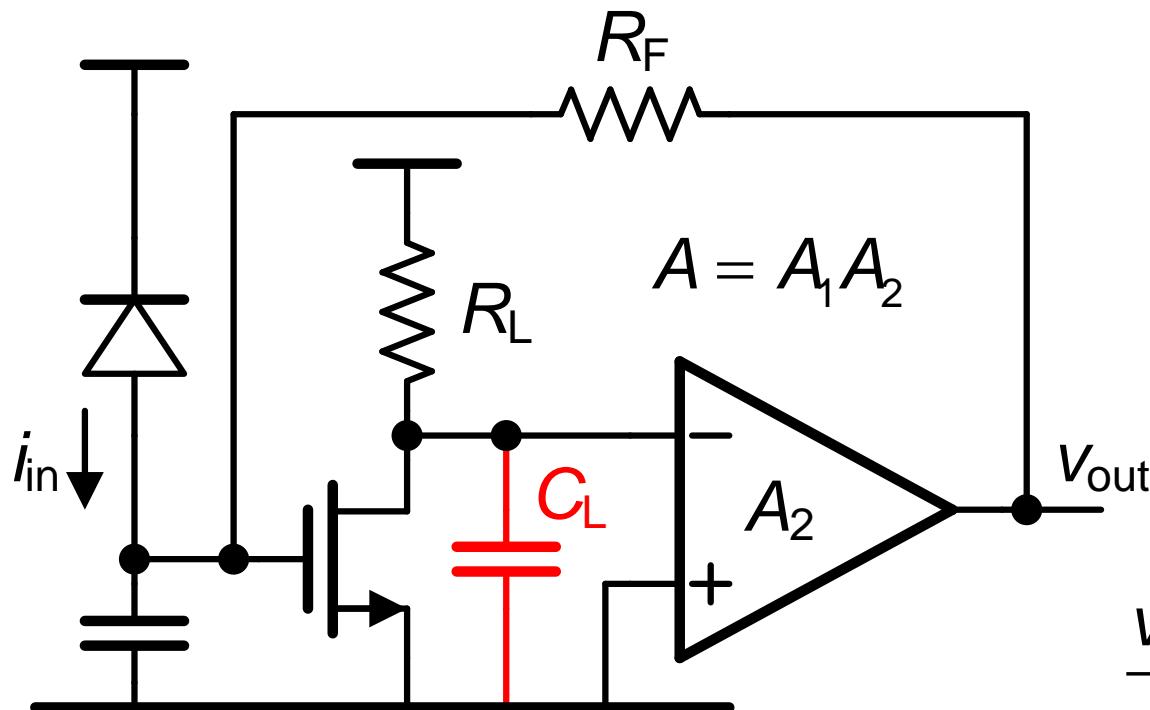
$$\frac{V_{in}}{i_{in}} = \frac{1}{sC_p} // \frac{R_F}{A_1 A_2}$$

$$= \frac{R_F}{A_1 A_2} \frac{1}{1 + R_F \frac{C_p}{A_1 A_2} s}$$

$$\frac{V_{out}}{i_{in}} = R_F \frac{1}{1 + R_F \frac{C_p}{A_1 A_2} s}$$

$$A_R BW(\text{THz}\Omega) = \frac{A_1 A_2}{2\pi C_p}$$

接电压放大器的电流检测器 2



$$\frac{V_{in}}{i_{in}} = \frac{R_F}{A_1 A_2} \frac{1 + R_L C_L s}{1 + as + bs^2}$$

$$a = \frac{R_F C_p}{A_1 A_2}$$

$$b = \frac{R_F C_p R_L C_L}{A_1 A_2}$$

$$\frac{V_{out}}{i_{in}} = R_F \frac{1}{1 + as + bs^2}$$

如果 $R_L < \sqrt{\frac{R_F}{4g_m A_2}} \frac{C_p}{C_L}$, 则没有峰值

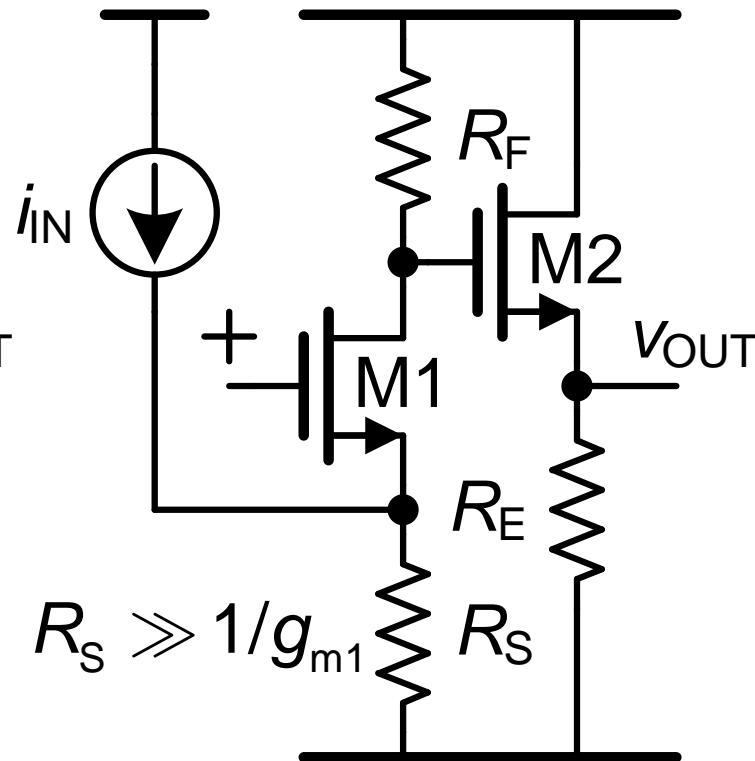
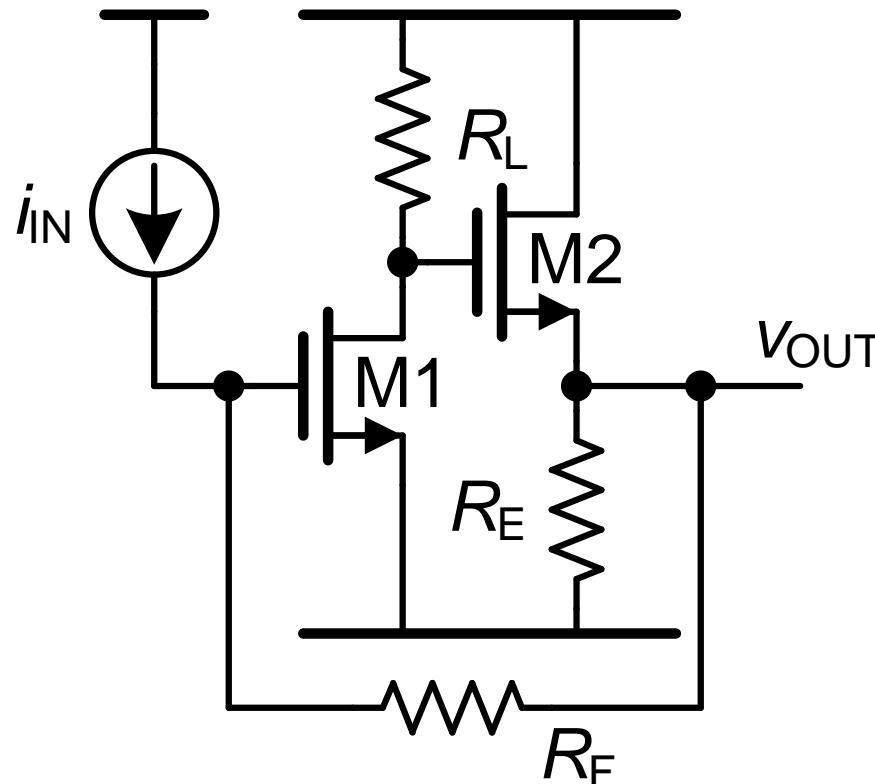
接电压放大器的电流检测器 3

$$\frac{V_{in}}{I_{in}} = \frac{R_F}{\frac{A_1}{1 + R_L C_L s} A_2} \frac{1}{1 + R_F \frac{C_p}{\frac{A_1}{1 + R_L C_L s} A_2} s}$$

$$= \frac{R_F}{A_1 A_2} \frac{1 + R_L C_L s}{1 + \frac{R_F C_p}{A_1 A_2} s + \frac{R_F C_p R_L C_L}{A_1 A_2} s^2}$$

$$\left(\frac{R_F C_p}{A_1 A_2} \right)^2 - 4 \frac{R_F C_p R_L C_L}{A_1 A_2} > 0 \xrightarrow{A_1 = g_m R_L} R_L < \sqrt{\frac{R_F}{4 g_m A_2} \frac{C_p}{C_L}}$$

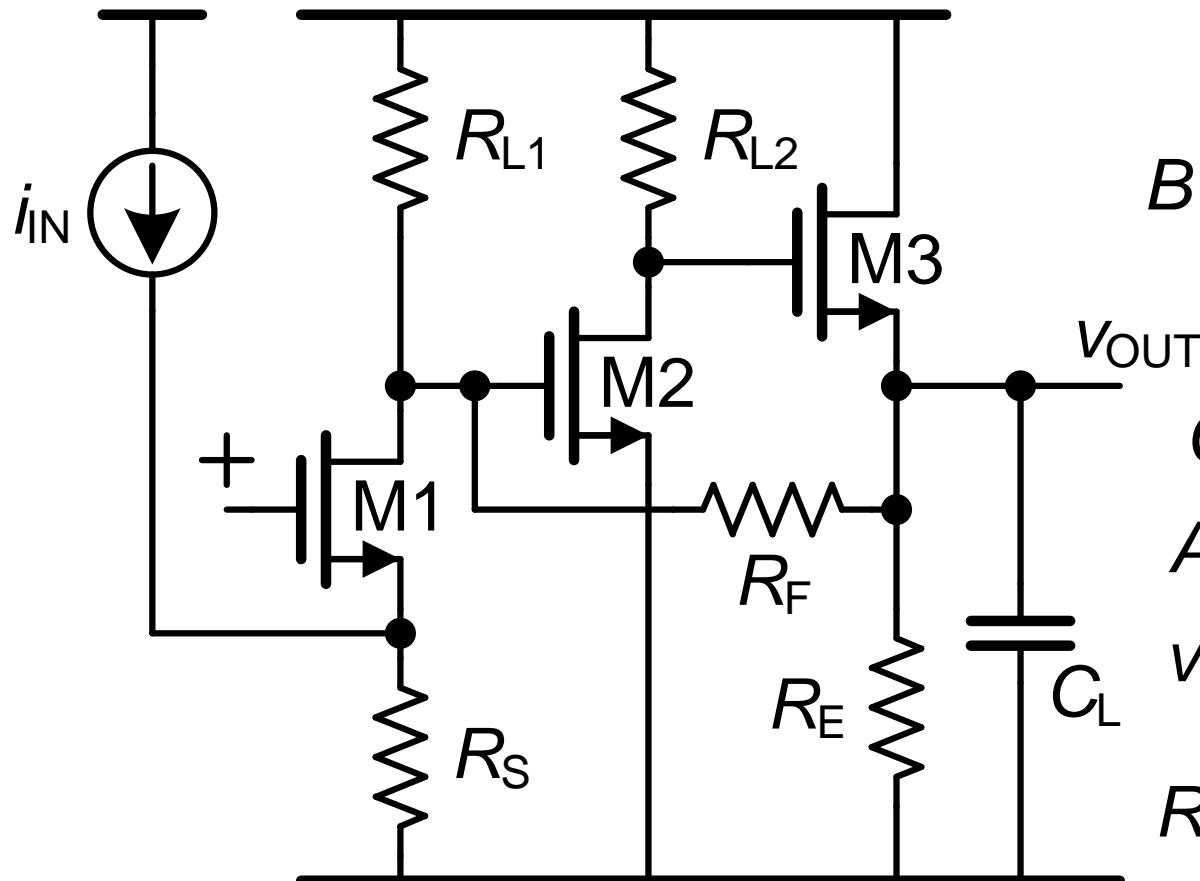
电压/电流放大器的带宽: BW



$$BW = \frac{A_{V1}}{2\pi R_F(C_{GS1} + C_D + A_{V1}C_{GD1})}$$

$$BW = \frac{1}{2\pi R_F(C_{DG2} + C_{DB1})}$$

接共源共栅输入的电流检测器



Z_{in} 与 f 无关!

$$R_S \gg 1/g_{m1}$$

$$BW = \frac{1}{2\pi \left(\frac{R_F // R_{L1}}{A_{V2}} \right) C_T}$$

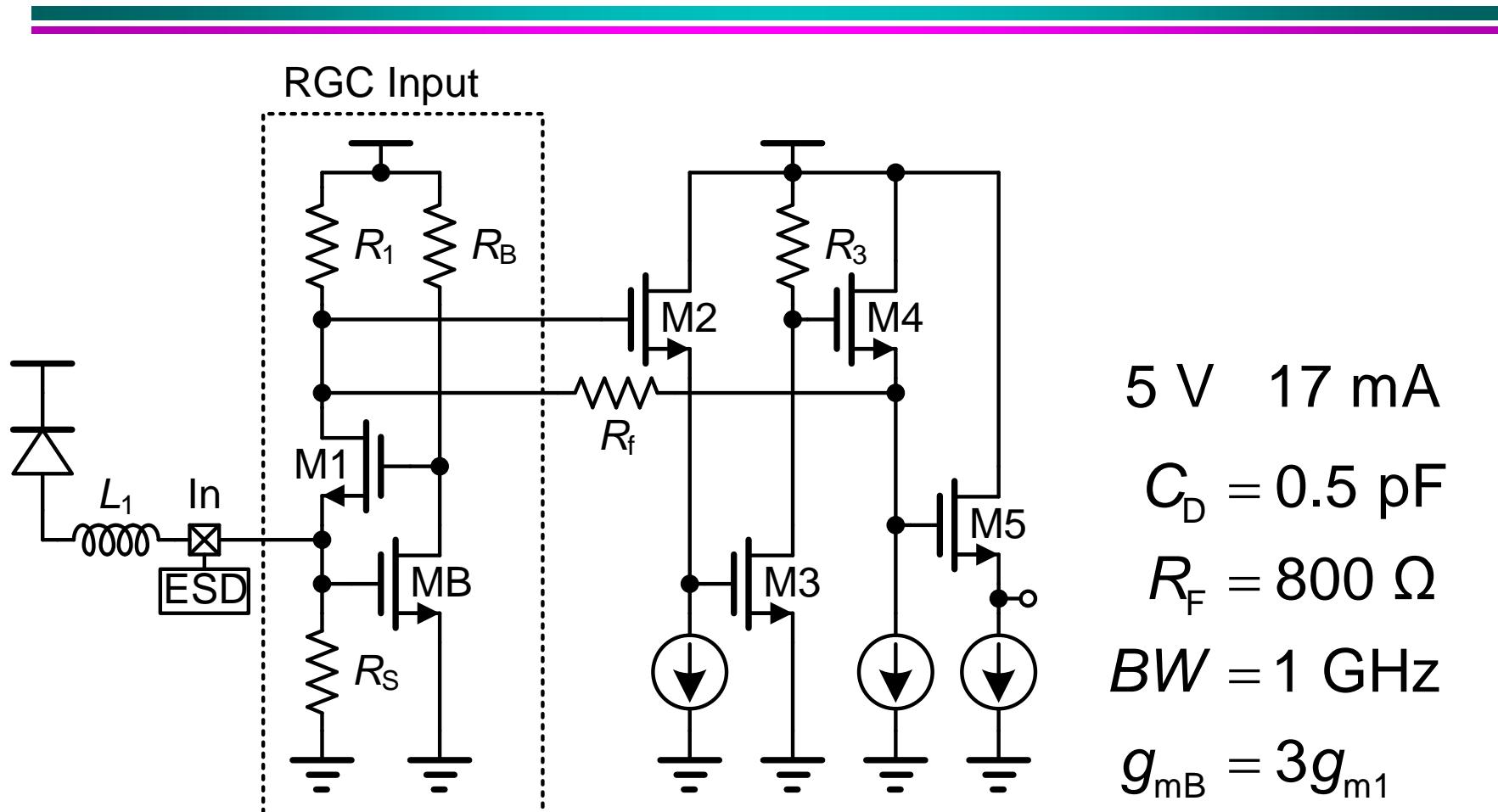
$$C_T = C_{GS2} + A_{V2} C_{GD2}$$

$$A_{V2} = g_{m2} R_{L2}$$

$$V_{out} = R_F i_{in}$$

$$R_{out} = \frac{1/g_{m3}}{A_{V2}}$$

Ref.: Vanisri, et al, JSSC June 95, pp. 677-685

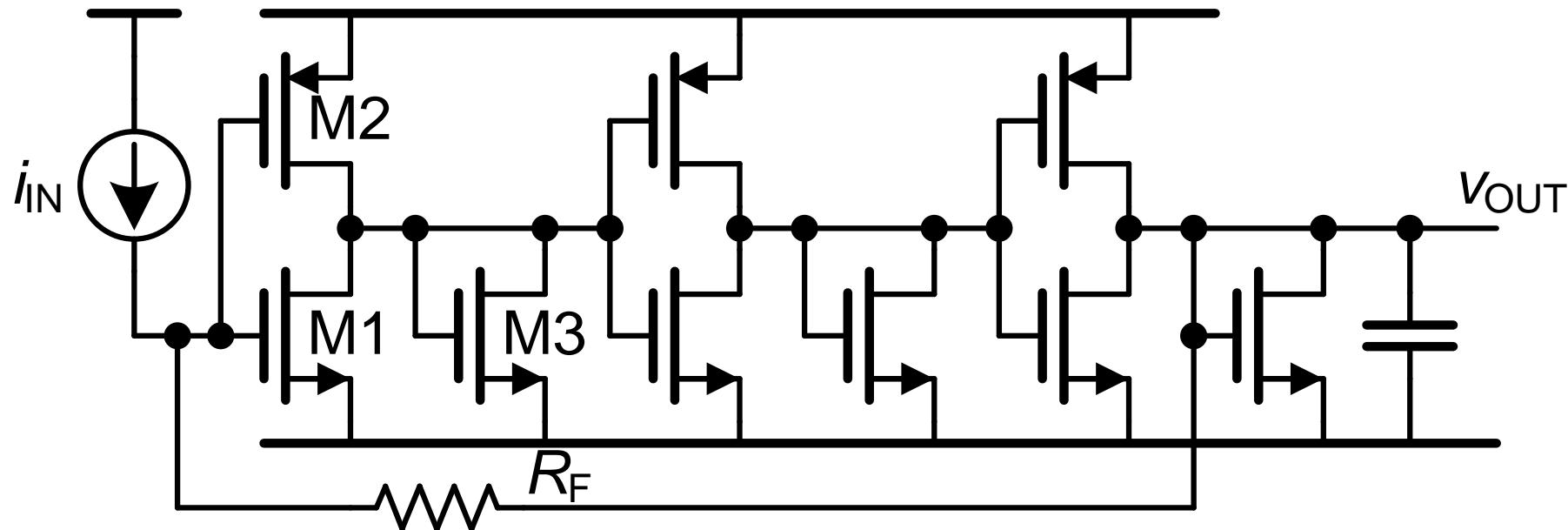


BW 与 C_D 无关!

电流噪声: R_S 和 $R_F//R_1$

Ref.: Vanisri, et al, JSSC June 95, pp. 677-685

CMOS光敏二极管放大器

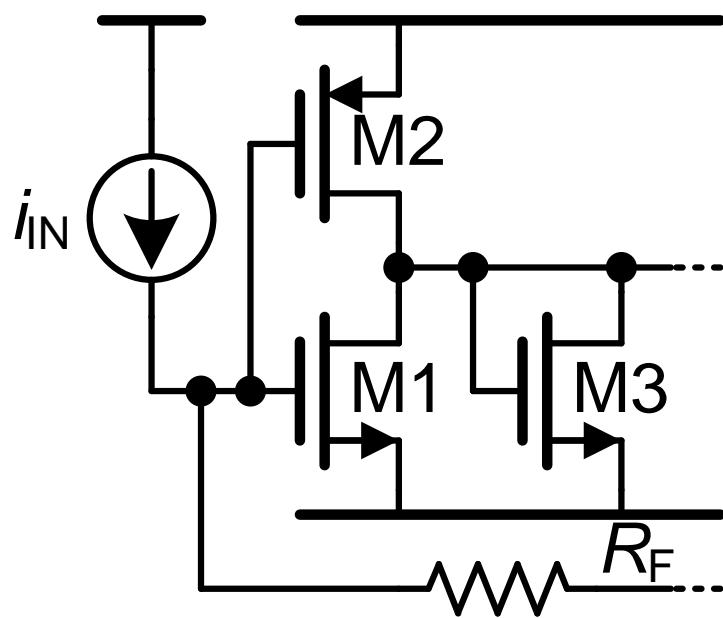


$$150 \text{ K}\Omega \times 120 \text{ MHz} = 18 \text{ THz}\Omega \quad 0.5 \text{ pA}/\sqrt{\text{Hz}}$$

450 MHz per cell

Ref.: Ingels, JSSC Dec 1994, 1552-1559

CMOS宽带放大器核心单元



$$I_{DS1} = \lambda I_{DS2} \quad I_{DS3} = (1 - \lambda) I_{DS2}$$

M1和M3: 有相同的 V_{GS} 和 V_{DS}

$$K_n' \approx 2K_p'$$

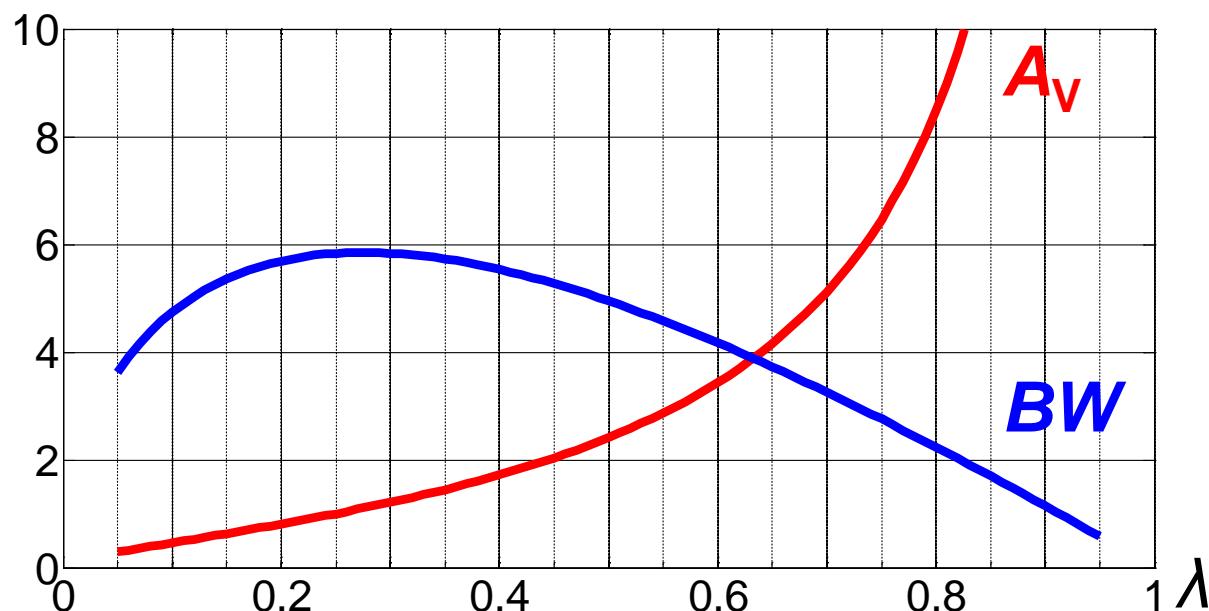
所有 L 均为 L_{min}

$$A_v = \frac{g_{m1} + g_{m2}}{g_{m3}}$$

$$g_m = 2\sqrt{K_n' I_{DS} W/L}$$

$$V_{GS1} = V_{GS3} : W_3 = W_1 \frac{1 - \lambda}{\lambda}$$

CMOS宽带放大器: 增益和带宽



$$\frac{\lambda}{1-\lambda} \left(1 + \sqrt{\frac{W_2}{2\lambda W_1}} \right)$$

$$BW = \frac{g_{m3}}{2\pi C_n}$$

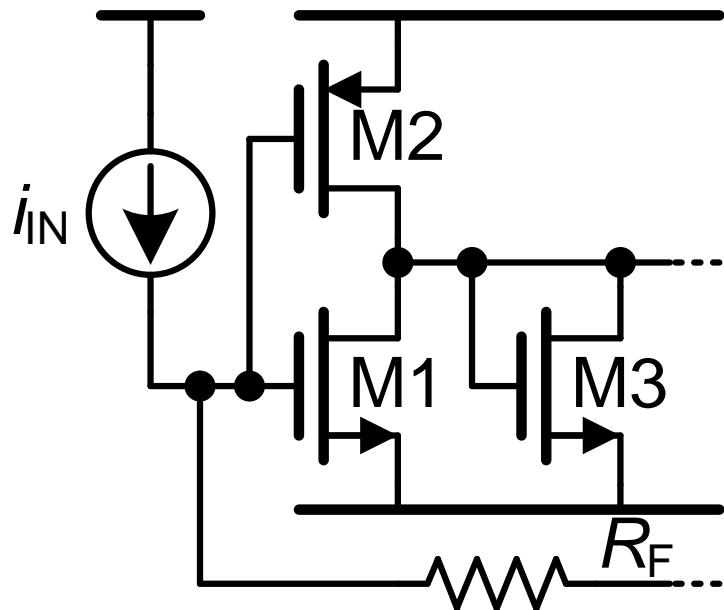
$$\sim \frac{(1-\lambda)\sqrt{\lambda W_1}}{W_1(2-\lambda) + \lambda W_2}$$

$$W_1 = 2 \quad W_2 = 4$$

$$C_n = C_{DB1} + C_{GS3} + C_{DB3} + C_{DB2}$$

$$C_{DB} \approx C_{GS} \approx kW \quad k \approx 2 \text{ fF}/\mu\text{m}$$

集成电阻



R_F ? 多晶硅电阻：大尺寸：长 L
分布电容：
在100 MHz处45°相移

$$f_{-3\text{dB}} = \frac{1}{2\pi} \frac{2.43}{R_s C_0 L^2}$$

R_s = sheet res. (Ω/\square)

C_0 = unit cap. (F/cm^2)

MOST : $W = 1.3 \mu\text{m}$ & $L = 1 \mu\text{m}$

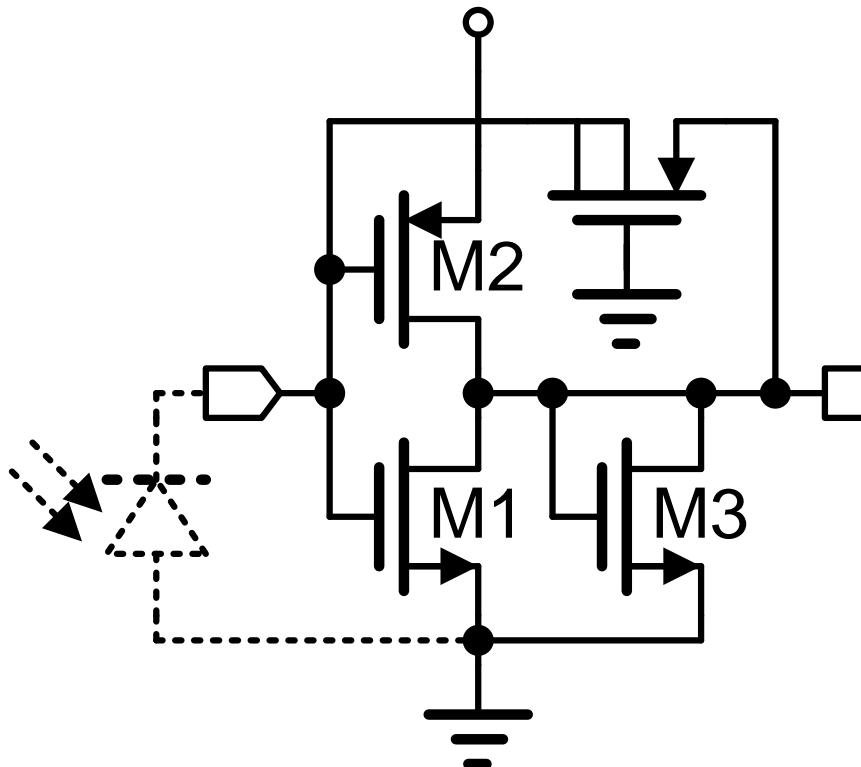
允许动态压缩

Ref.: Glaser; IC Engineering Add.Wesley, p.132

1 Gb/s 1 KΩ 跨导级

$$C_d = 0.8 \text{ pF} \approx C_{GS}$$

容性噪声匹配!



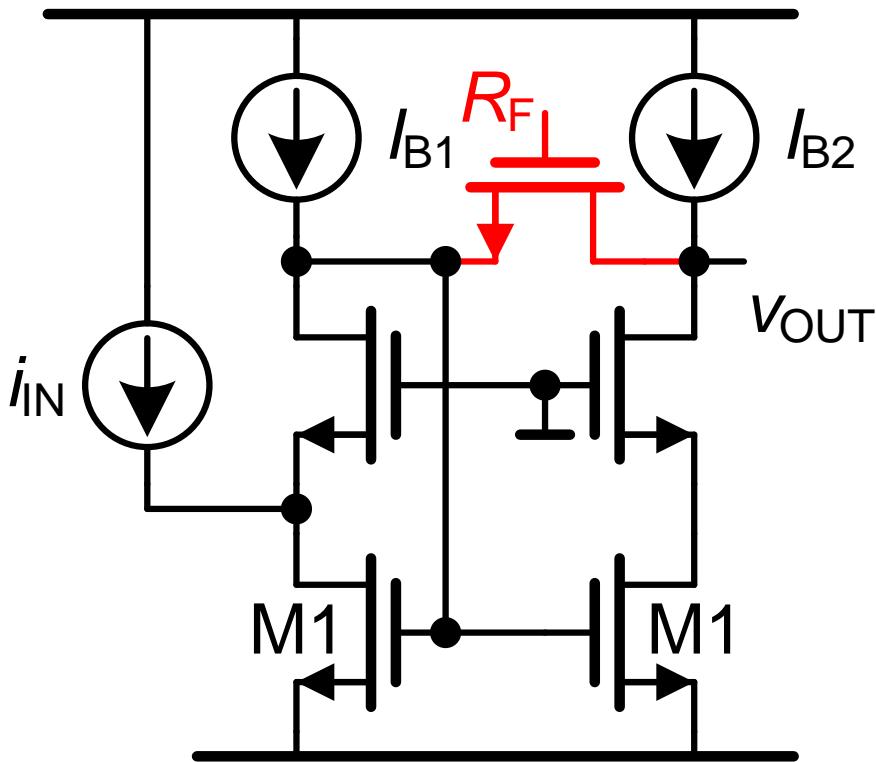
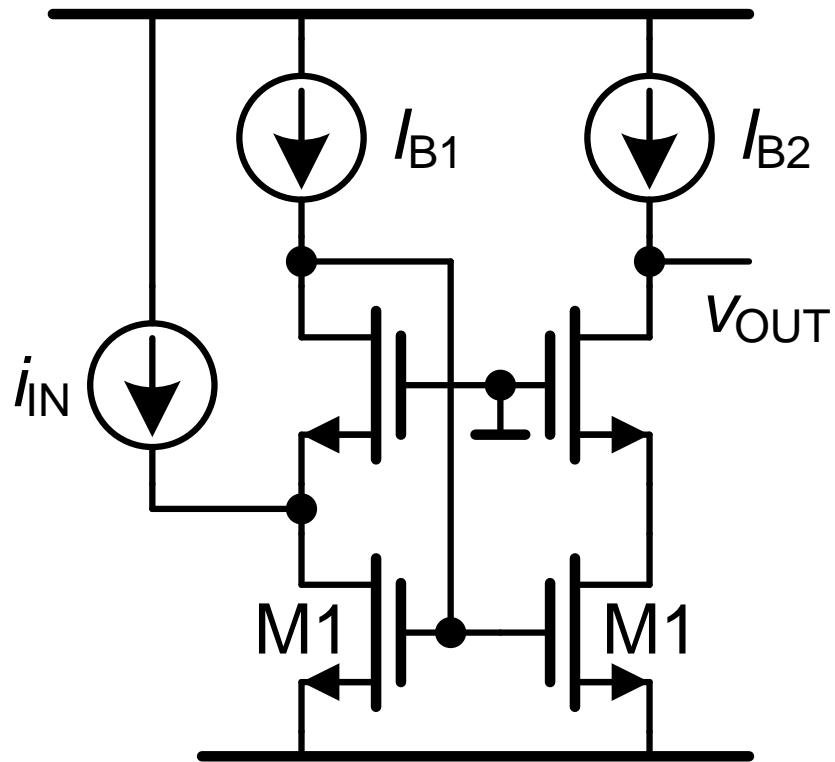
$$BW = 500 \text{ MHz}$$

$$5 \text{ mA (5V)}$$

$$0.7 \mu\text{m CMOS}$$

Ref.: Ingels, JSSC July 1999, 971-977

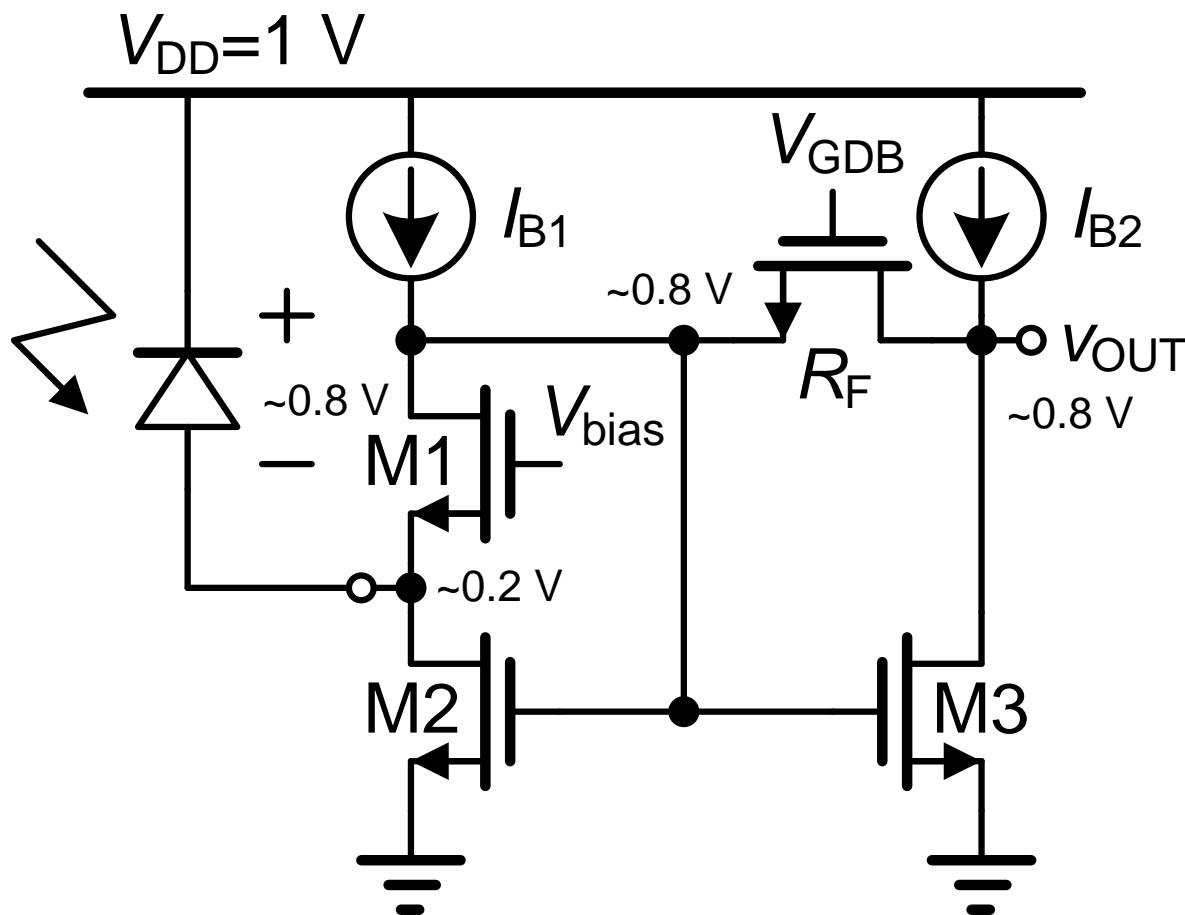
低电压跨阻放大器



如果 $R_F > 1/g_{m1}$: $V_{out} = -R_F i_{in}$

Ref.: Phang, Johns, ISSCC 2001, 218-219

75 Mb/s CMOS光接收器



Ref.: Phang, Johns, ISSCC 2001, 218-219